

Two angles are **complementary angles** if the sum of their measure is  $90^\circ$ . Each angle is the **complement** of the other.

Two angles are **supplementary angles** if the sum of their measure is  $180^\circ$ . Each angle is the **supplement** of the other.

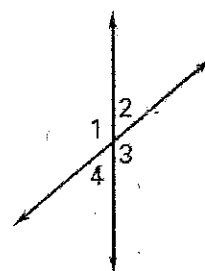
Two angles are **vertical angles** if their sides form two pairs of opposite rays.

Two adjacent angles are a **linear pair** if their noncommon sides are opposite rays.

**Adjacent angles** are two angles that share a common ray. They are next to each other.

**EXAMPLE 1** Identifying Vertical Angles and Linear Pairs

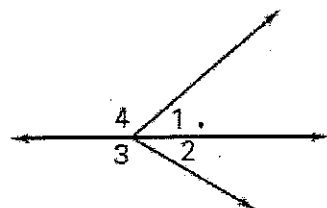
- a. Are  $\angle 1$  and  $\angle 3$  vertical angles? *yes*
- b. Are  $\angle 2$  and  $\angle 4$  a linear pair? *no*
- c. Are  $\angle 1$  and  $\angle 4$  a linear pair? *yes*



Exercises for Example 1

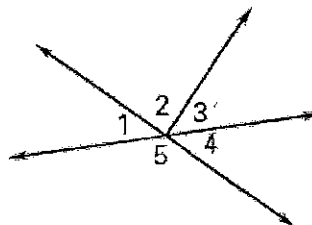
Use the figure to answer the questions.

1.



- a. Are  $\angle 1$  and  $\angle 2$  a linear pair? *no*
- b. Are  $\angle 1$  and  $\angle 3$  vertical angles? *no*
- c. Are  $\angle 1$  and  $\angle 4$  a linear pair? *yes*
- d. Are  $\angle 2$  and  $\angle 4$  vertical angles? *no*

2.

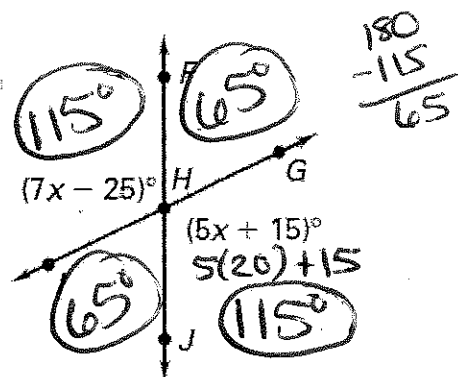


- a. Are  $\angle 1$  and  $\angle 5$  a linear pair? *yes*
- b. Are  $\angle 1$  and  $\angle 2$  a linear pair? *no*
- c. Are  $\angle 1$  and  $\angle 4$  vertical angles? *yes*
- d. Are  $\angle 3$  and  $\angle 5$  vertical angles? *no*

**EXAMPLE 2** Finding Angle Measures

Solve for  $x$  in the diagram at the right.  
Then find the angle measures.

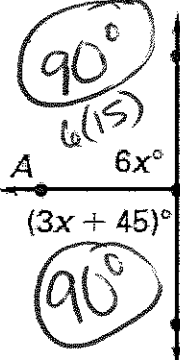
$$\begin{array}{r}
 7x - 25 = 5x + 15 \\
 -5x \quad -5x \\
 \hline
 2x - 25 = 15 \\
 +25 \quad +25 \\
 \hline
 2x = 40 \\
 \frac{2x}{2} = \frac{40}{2} \\
 x = 20
 \end{array}$$



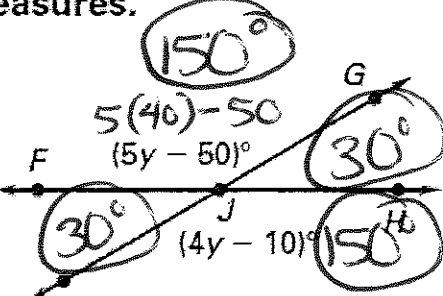
LP: Angle + Angle = 180  
 vertical: Angle = Angle

**Exercises for Example 2**

Solve for x and y, then find the angle measures.

3. 

$$\begin{aligned} 6x + 3x + 45 &= 180 \\ 9x + 45 &= 180 \\ -45 & \quad -45 \\ \hline 9x &= 135 \\ \frac{9x}{9} &= \frac{135}{9} \\ x &= 15 \end{aligned}$$

4. 

$$\begin{aligned} 5(40) - 50 &= 4y - 10 \\ (5y - 50) &= 4y - 10 \\ -4y & \quad -4y \\ \hline y - 50 &= -10 \\ y + 50 & \quad +50 \\ \hline y &= 40 \end{aligned}$$

**EXAMPLE 3** Finding Measures of Complements and Supplements

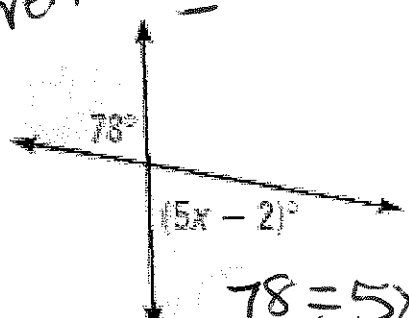
- a. Given that  $\angle E$  is a complement of  $\angle F$  and  $m\angle E = 68^\circ$ , find  $m\angle F$ .  $90^\circ - 68^\circ = 22^\circ$
- b. Given that  $\angle G$  is a supplement of  $\angle H$  and  $m\angle G = 152^\circ$ , find  $m\angle H$ .  $180^\circ - 152^\circ = 28^\circ$

**Exercises for Example 3**

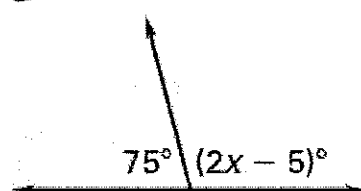
Find the measure of the angle.

5. Given that  $\angle A$  is a complement of  $\angle B$  and  $m\angle B = 81^\circ$ , find  $m\angle A$ .  $90 - 81 = 9^\circ$
6. Given that  $\angle C$  is a supplement of  $\angle D$  and  $m\angle C = 27^\circ$ , find  $m\angle D$ .  $180 - 27 = 153^\circ$

~~TOTD~~: Solve for x in each of the following:

7. vertical = 

$$\begin{aligned} 78 &= 5x - 2 \\ +2 & \quad +2 \\ \hline 80 &= 5x \\ \frac{80}{5} &= \frac{5x}{5} \\ 16 &= x \end{aligned}$$

8. LP supp = 180 

$$\begin{aligned} 75 + 2x - 5 &= 180 \\ 70 + 2x &= 180 \\ -70 & \quad -70 \\ \hline 2x &= 110 \\ \frac{2x}{2} &= \frac{110}{2} \\ x &= 55 \end{aligned}$$