

Trig - Sin/Cos Relationship

Name: Key

What does complementary mean?

Use your calculator to find the value of the following (Round to the nearest 3 decimals):

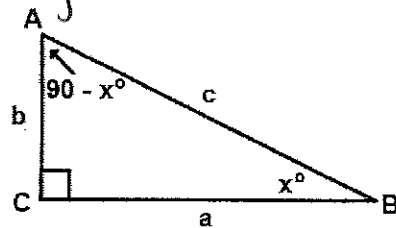
1. $\sin 30^\circ = \underline{.5}$ $\cos 60^\circ = \underline{.5}$
2. $\cos 21^\circ = \underline{.934}$ $\sin 69^\circ = \underline{.934}$
3. $\cos 38^\circ = \underline{.788}$ $\sin 52^\circ = \underline{.788}$
4. $\sin 45^\circ = \underline{.707}$ $\cos 45^\circ = \underline{.707}$

Based on the above calculations, what do you think $\sin 13^\circ$ would be equivalent to? $\cos \underline{77^\circ}$

Can you come up with a rule that would work every time? *sin/cos functions that are complementary are congruent.*

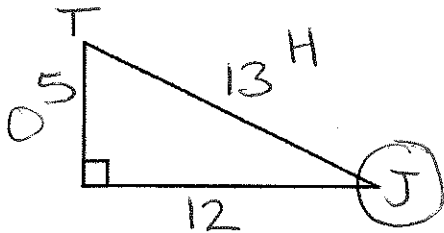
Sin / Cos Relationship

$\sin A = \cos (90 - A)$ $\sin \theta = \cos (90 - \theta)$
 $\cos A = \sin (90 - A)$ $\cos \theta = \sin (90 - \theta)$



Using the Sin / Cos relationship:

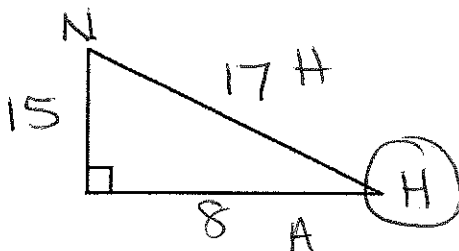
1. If Angle T and Angle J are complementary angles in a right triangle and $\sin T = \frac{12}{13}$, what is $\sin J$?



$$\begin{aligned}
 12^2 + x^2 &= 13^2 \\
 144 + x^2 &= 169 \\
 \underline{-144} \quad \underline{-144} \\
 x^2 &= 25 \\
 x &= \sqrt{25} = 5
 \end{aligned}$$

$$\begin{aligned}
 \sin T &= \frac{O}{H} = \frac{12}{13} \\
 \sin J &= \frac{O}{H} = \frac{5}{13}
 \end{aligned}$$

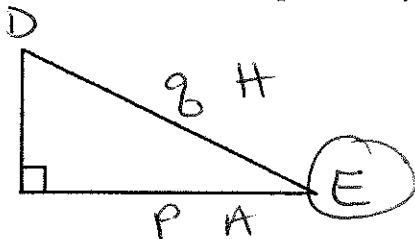
2. If Angle N and Angle H are complementary angles in a right triangle and $\cos N = \frac{15}{17}$, what is $\cos H$?



$$\begin{aligned}
 15^2 + x^2 &= 17^2 \\
 225 + x^2 &= 289 \\
 \underline{-225} \quad \underline{-225} \\
 x^2 &= 64 \\
 x &= \sqrt{64} = 8
 \end{aligned}$$

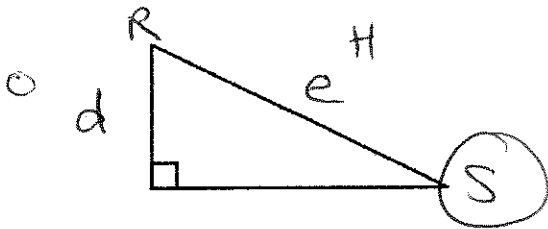
$$\begin{aligned}
 \cos N &= \frac{A}{H} = \frac{15}{17} \\
 \cos H &= \frac{A}{H} = \frac{8}{17}
 \end{aligned}$$

3. Angle D and E are complementary angles. If $\sin D = \frac{p}{q}$, what is $\cos E$?



$$\begin{aligned}
 \sin D &= \frac{O}{H} = \frac{p}{q} \\
 \cos E &= \frac{A}{H} = \frac{p}{q}
 \end{aligned}$$

4. Angle R and S are complementary angles. If $\cos R = \frac{d}{e}$, what is $\sin S$?



$$\cos R = \frac{A}{H} = \frac{d}{e}$$

$$\sin S = \frac{O}{H} = \frac{d}{e}$$

5. In $\triangle ABC$, the $m\angle B = 90^\circ$. For what value of x does $\sin(x - A) = \cos A$?

a. 0°

b. 45°

c. 90°

d. 180°

6. Which of the following is equivalent to $\cos 35^\circ$?

a. $\sin 35^\circ$

b. $\sin 55^\circ$

c. $\cos 55^\circ$

d. $\sin 145^\circ$

7. Which of the following is equivalent to $\sin 50^\circ$?

a. $\cos 50^\circ$

b. $\sin 40^\circ$

c. $\cos 40^\circ$

d. $\cos 130^\circ$

8. Which of the following is equivalent to $\sin 15^\circ$?

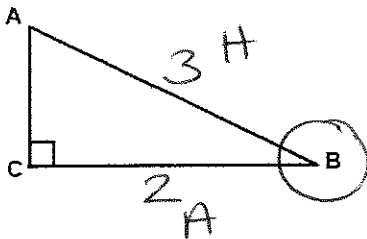
a. $\cos 15^\circ$

b. $\sin 75^\circ$

c. $\cos 75^\circ$

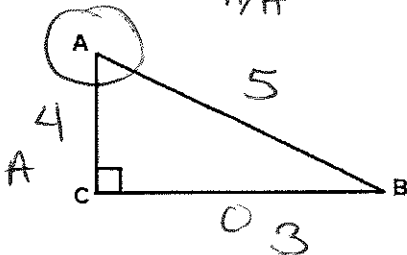
d. $\sin 15^\circ$

9. If the $\sin A = \frac{2}{3}$, what is the $\cos B$? = $\frac{A}{H}$



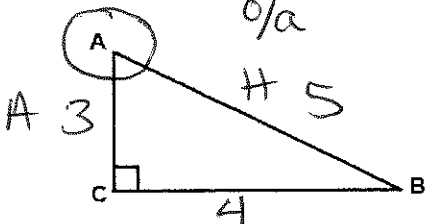
$$\frac{2}{3}$$

10. If the $\cos A = \frac{4}{5}$, what is the $\tan A$? = $\frac{O}{A} = \frac{3}{4}$



$$\begin{array}{r} 4^2 + x^2 = 5^2 \\ 16 + x^2 = 25 \\ \hline -16 \quad \quad -16 \\ \hline x^2 = 9 \\ x = \sqrt{9} = 3 \end{array}$$

11. If the $\tan A = \frac{4}{3}$, what is the $\cos A$? = $\frac{A}{H} = \frac{3}{5}$



$$\begin{array}{r} 3^2 + 4^2 = c^2 \\ 9 + 16 = c^2 \\ 25 = c^2 \\ \sqrt{25} = c \\ 5 = c \end{array}$$