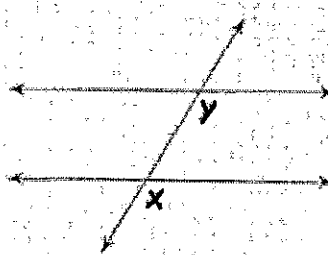
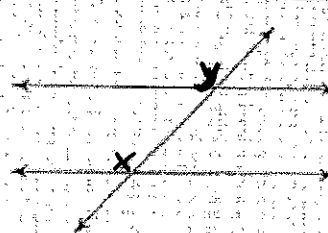
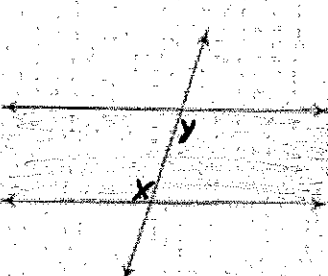


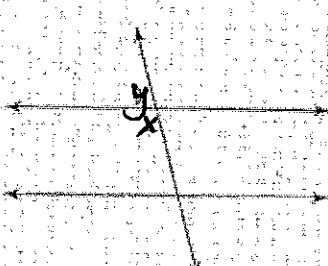
Parallel Lines & Transversals

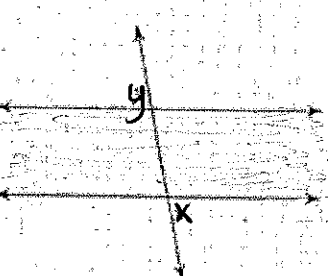
Identify each pair of angles as corresponding, alternate interior, alternate exterior, same-side interior, vertical, or adjacent. Then identify as supplementary, complementary, or a linear pair.

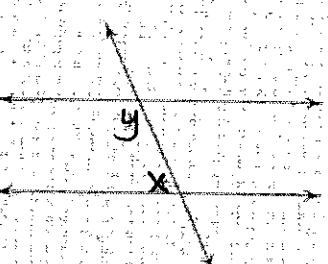
1)  corresponding

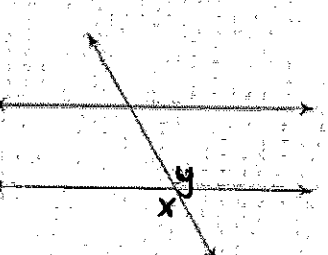
2)  corresponding

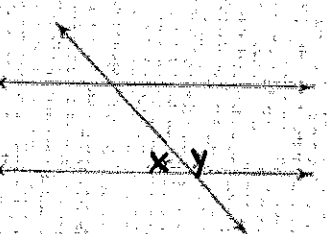
3)  Alternate Interior

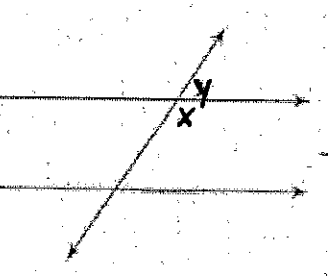
4)  Linear Pair  
ALSO Adjacent

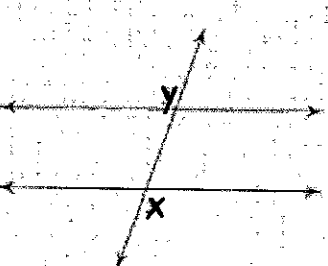
5)  Alternate Exterior

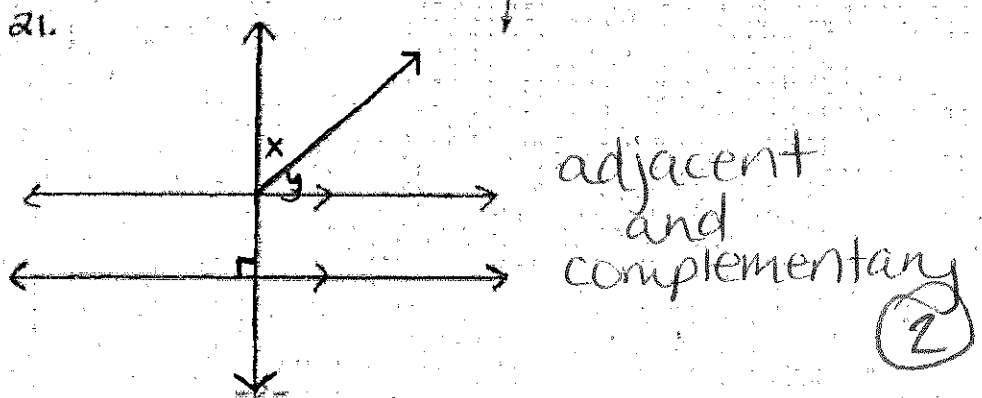
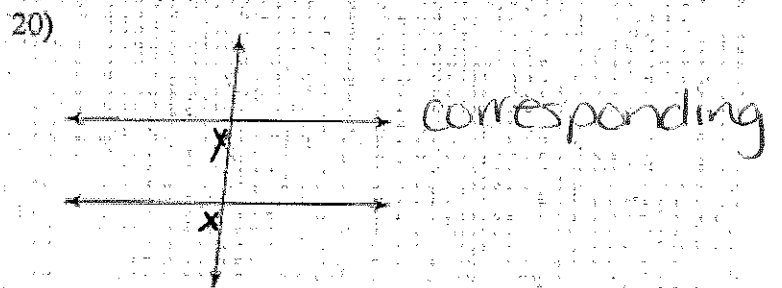
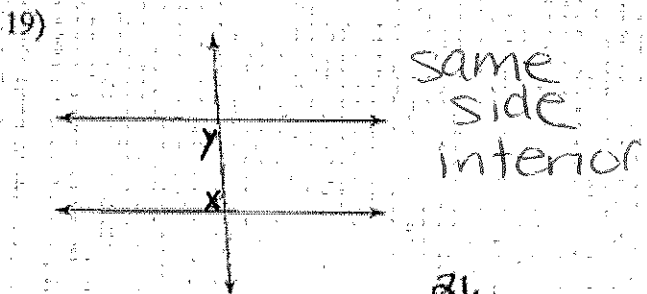
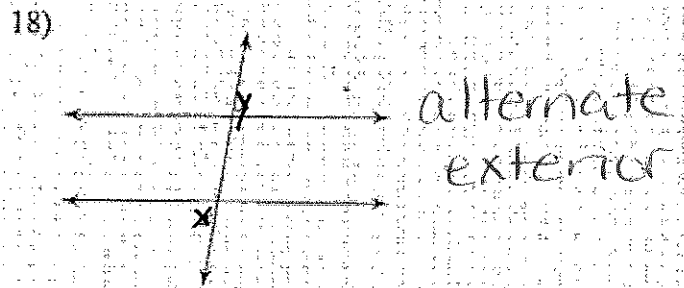
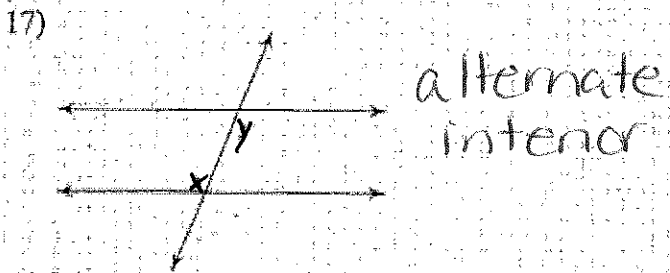
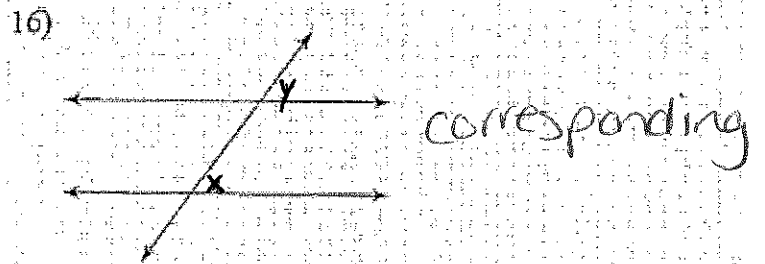
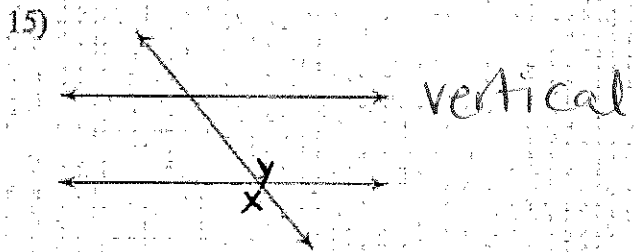
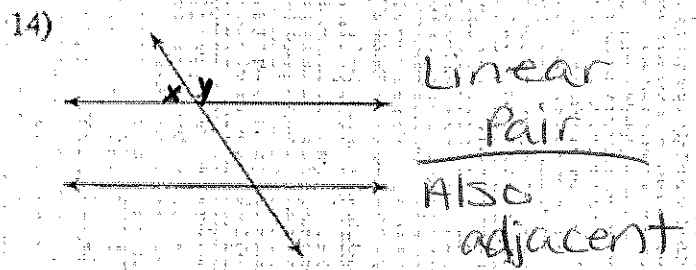
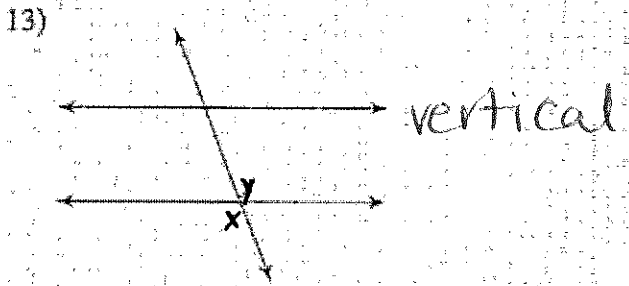
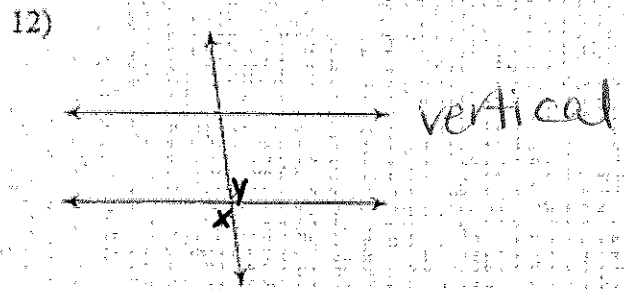
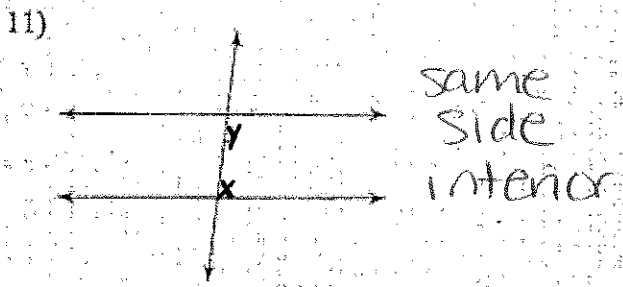
6)  same side interior

7)  vertical

8)  Linear Pair  
ALSO Adjacent

9)  Linear Pair  
ALSO Adjacent

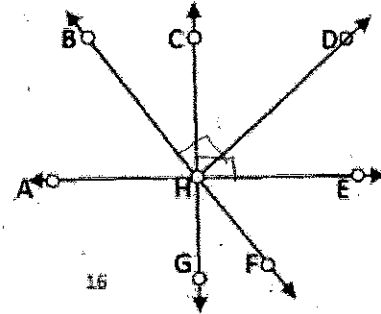
10)  Alternate Exterior



PROBLEMS

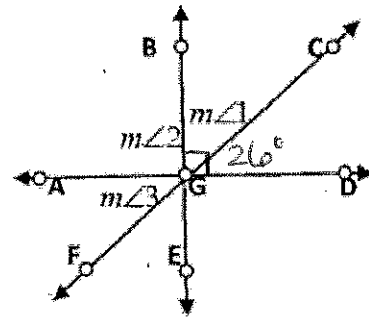
Copy and complete the statement given that  $m\angle BHD = m\angle CHE = 90^\circ$ .

1.  $m\angle AHG = 90^\circ$
2.  $m\angle CHA = 90^\circ$
3. If  $m\angle CHD = 31^\circ$ , then  $m\angle DHE = 59^\circ$   $90 - 31 = \text{comp.}$
4. If  $m\angle BHA = 48^\circ$ , then  $m\angle EHF = 48^\circ$  vertical  $\angle$ 's
5. If  $m\angle GHF = 38^\circ$ , then  $m\angle AHB = 52^\circ$   $90 - 38 = 52^\circ$   
complementary and then vertical



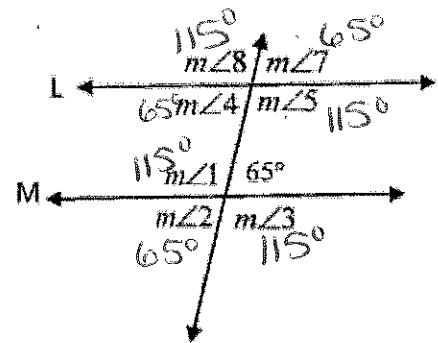
If  $m\angle BGD = 90^\circ$  and  $m\angle CGD = 26^\circ$ , find

6.  $m\angle 1$   $90 - 26 = 64^\circ$  complementary
7.  $m\angle 2$   $180 - 90 = 90^\circ$  supplementary
8.  $m\angle 3$   $26^\circ$  vertical  $\angle$ 's are  $\cong$
9.  $m\angle FGE =$  to  $\angle 1$  so  $64^\circ$  vertical
10.  $m\angle DGE$   $180 - 90 = 90^\circ$  supplementary



Lines L and M are parallel, find

11.  $m\angle 1$   $115^\circ$
12.  $m\angle 2$   $65^\circ$
13.  $m\angle 3$   $115^\circ$
14.  $m\angle 4$   $65^\circ$
15.  $m\angle 5$   $115^\circ$
16.  $m\angle 6$   $65^\circ$
17.  $m\angle 7$   $65^\circ$
18.  $m\angle 8$   $115^\circ$



$180 - 65$   
 $115$

PROBLEMS:

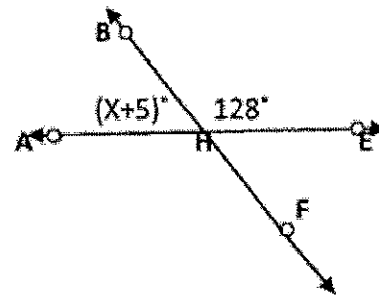
11. Solve for  $x$  in the diagram Justify

$$x + 5 + 128 = 180$$

$$x + 133 = 180$$

$$\underline{-133 \quad -133}$$

$x = 47$  linear pairs are supplementary



12. Solve for  $x$  in the diagram Justify

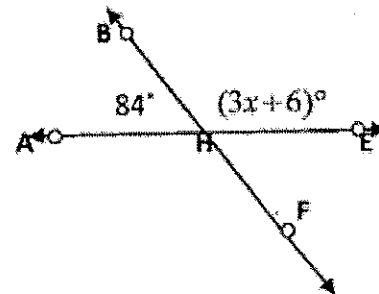
$$84 + 3x + 6 = 180$$

$$90 + 3x = 180$$

$$\underline{-90 \quad -90}$$

$$\frac{3x = 90}{3 \quad x}$$

$x = 30$  linear pairs are supplementary



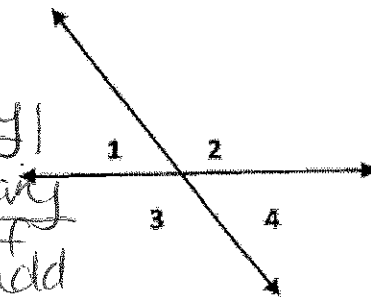
Use the diagram to decide whether the statement is true or false.

13. If  $m\angle 1 = 47^\circ$ , then  $m\angle 2 = 43^\circ$ . False, linear pairs are supplementary, not complementary.

14. If  $m\angle 1 = 47^\circ$ , then  $m\angle 3 = 47^\circ$ . False, not congruent, they are supplementary.

15.  $m\angle 1 + m\angle 3 = m\angle 2 + m\angle 4$ . True, both are sets of linear pairs that add up to  $180^\circ$ .

16.  $m\angle 1 + m\angle 4 = m\angle 2 + m\angle 3$ . False, both are vertical  $\angle$ 's but the sets are not = to each other.

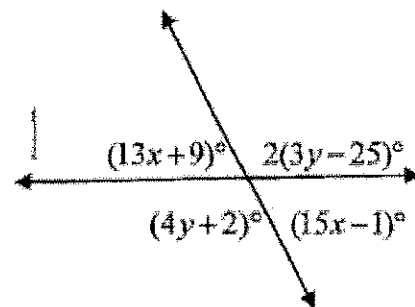


Find the value of the variable.

Using vertical  $\angle$ 's are  $\cong$

$$\begin{array}{r} 13x + 9 = 15x - 1 \\ -13x \quad -13x \\ \hline 9 = 2x - 1 \\ +1 \quad +1 \\ \hline 10 = 2x \\ \frac{10}{2} = \frac{2x}{2} \\ x = 5 \end{array}$$

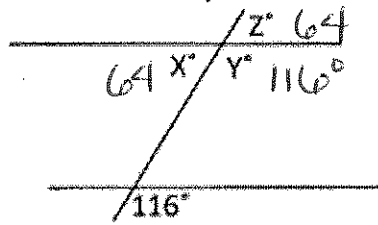
$$\left\{ \begin{array}{r} 4y + 2 = 2(3y - 25) \\ 4y + 2 = 6y - 50 \\ -4y \quad -4y \\ \hline 2 = 2y - 50 \\ +50 \quad +50 \\ \hline 52 = 2y \\ \frac{52}{2} = \frac{2y}{2} \\ y = 26 \end{array} \right.$$



4

17. Find the value of x, y, and z (the horizontal lines are parallel to each other)

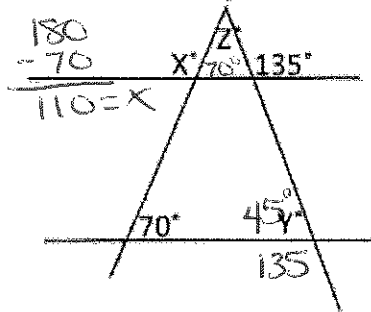
$x = \underline{64^\circ}$   
 $y = \underline{116^\circ}$   
 $z = \underline{64^\circ}$



$$\begin{array}{r} 180 \\ - 116 \\ \hline 64 \end{array}$$

18. Find the value of x, y, and z (the horizontal lines are parallel to each other)

$x = \underline{110^\circ}$   
 $y = \underline{45^\circ}$   
 $z = \underline{65^\circ}$

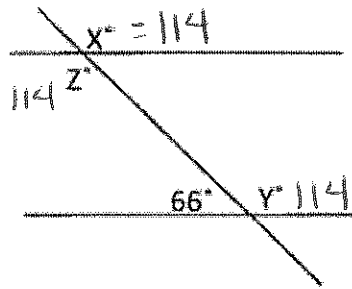


$$z \rightarrow \begin{array}{r} 180 \\ - 70 \\ - 45 \\ \hline 65 \end{array}$$

$$\begin{array}{r} 180 \\ - 135 \\ \hline 45 = y \end{array}$$

19. Find the value of x, y, and z (the horizontal lines are parallel to each other)

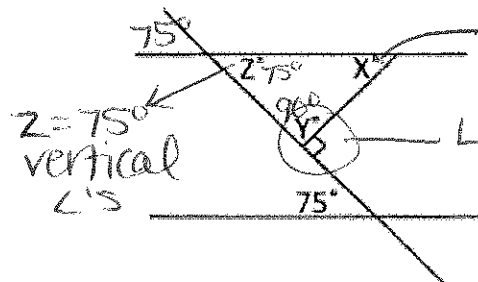
$x = \underline{114^\circ}$   
 $y = \underline{114^\circ}$   
 $z = \underline{114^\circ}$



$$\begin{array}{r} 180 \\ - 66 \\ \hline 114 = y \end{array}$$

20. Find the value of x, y, and z (the horizontal lines are parallel to each other)

$x = \underline{15^\circ}$   
 $y = \underline{90^\circ}$   
 $z = \underline{75^\circ}$



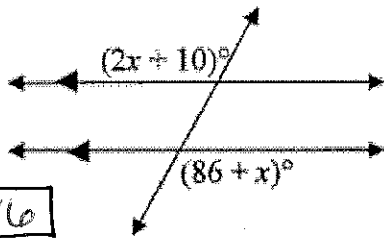
Δ's add up to 180 so...  
 $180 - 90 - 75 = 15$

Linear Pairs so  $y = 90$

$z = 75^\circ$   
 vertical  
 L's

Identify the type of angles and their relationship. Write the equation used to solve for x. Then, find the value of x. Put a box around your answer.

3.



$x = \boxed{76}$

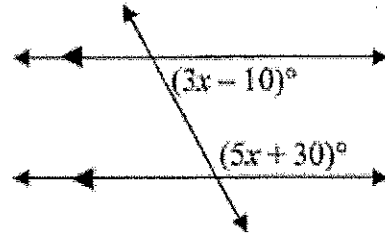
type of angles: Alt. Exterior

relationship: congruent

equation:  $2x + 10 = 86 + x$

$$\begin{array}{r} 2x + 10 = 86 + x \\ -x \quad -10 \quad -10 \quad -x \\ \hline x = 76 \end{array}$$

4.



$x = \boxed{20}$

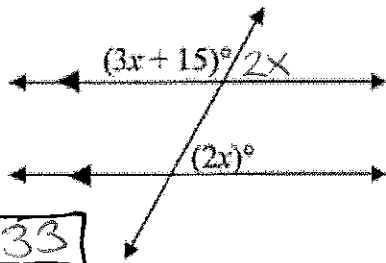
type of angles: same side interior

relationship: supplementary

equation:  $3x - 10 + 5x + 30 = 180$

$$\begin{array}{r} 8x + 20 = 180 \\ -20 \quad -20 \\ \hline 8x = 160 \\ \frac{8x}{8} = \frac{160}{8} \quad x = 20 \end{array}$$

5.



$x = \boxed{33}$

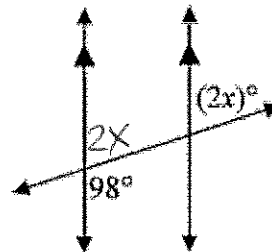
type of angles: Linear Pair of a corresponding angle

relationship: supplementary

equation:  $3x + 15 + 2x = 180$

$$\begin{array}{r} 5x + 15 = 180 \\ -15 \quad -15 \\ \hline 5x = 165 \\ \frac{5x}{5} = \frac{165}{5} \\ x = 33 \end{array}$$

6.



$x = \boxed{41}$

type of angles: Linear Pair of a corresponding angle

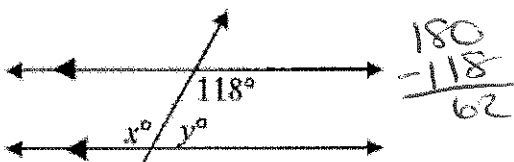
relationship: supplementary

equation:  $98 + 2x = 180$

$$\begin{array}{r} 2x = 82 \\ \frac{2x}{2} = \frac{82}{2} \\ x = 41 \end{array}$$

Find the values of x and y. Put a box around your answer.

7.

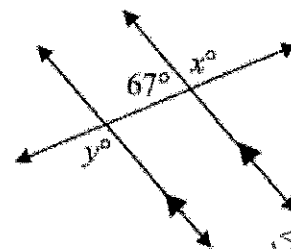


$$\begin{array}{r} 180 \\ -118 \\ \hline 62 \end{array}$$

$x = \boxed{118}$     $y = \boxed{62}$

alt. interior to  $118^\circ$  so =  
Linear pair to x or same side interior of  $118^\circ$  so supplementary

8.

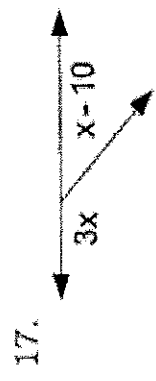
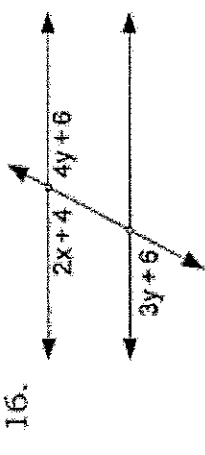
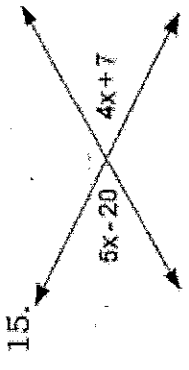
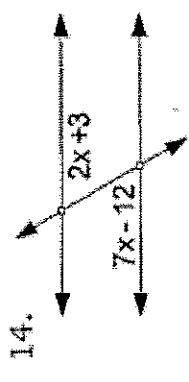
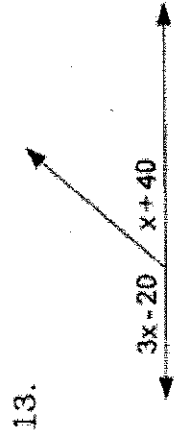
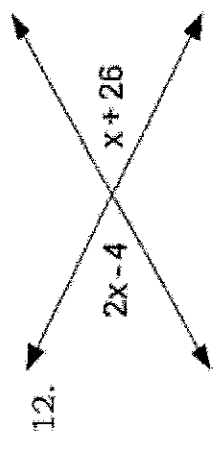
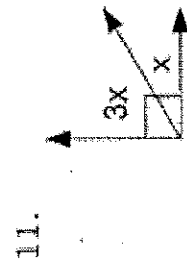
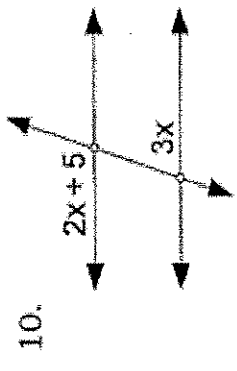
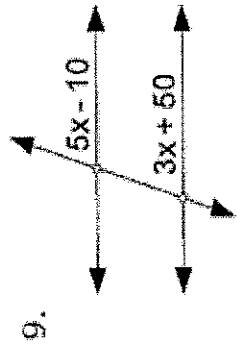
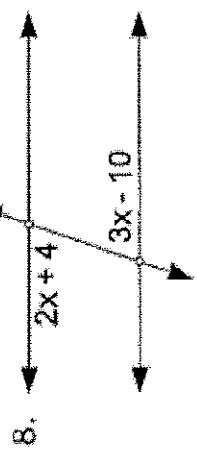
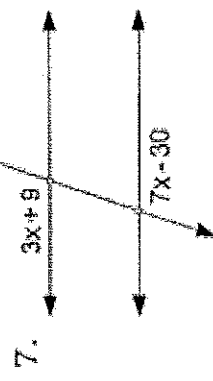
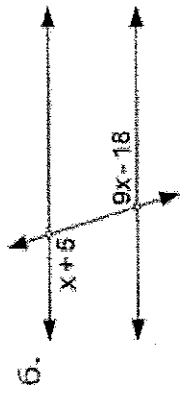
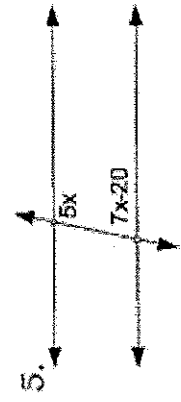
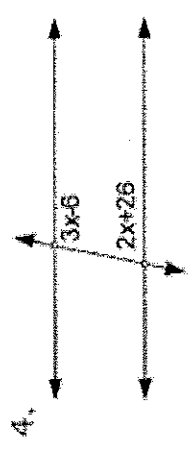
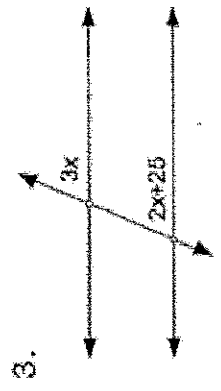
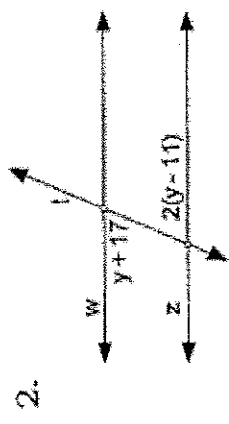
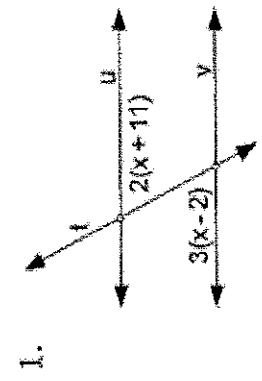


$x = \boxed{113}$  Linear pairs  
 $y = \boxed{113}$  alt. ext. to  $\angle x$ .

$$\begin{array}{r} 180 \\ -67 \\ \hline 113 \end{array}$$

$\boxed{6}$

Set up and solve each problem on notebook paper. Show steps for the Algebra. Assume lines that look parallel are. After finding the value of the variable, state the size of the angles.



For each... → set up and solve for variable (SHOW WORK)  
 → Tell the type of Angles they are and justify your answer (ex. vertical angles are  $\cong$ )  
 → substitute back in and tell the actual angle measures.

Page 7

$$\textcircled{1} \quad 2(x+11) = 3(x-2)$$

$$2x+22 = 3x-6$$

$$\begin{array}{r} -2x \quad -2x \\ \hline \end{array}$$

$$22 = x-6$$

$$\begin{array}{r} +6 \quad +6 \\ \hline \end{array}$$

$$\textcircled{28} = x$$

Alternate Interior

Angles are congruent

Each angle is  $60^\circ$   
or  $120^\circ$  accordingly.

$$\textcircled{2} \quad y+17 = 2(y-11)$$

$$y+17 = 2y-22$$

$$\begin{array}{r} -y \quad -y \\ \hline \end{array}$$

$$17 = y-22$$

$$\begin{array}{r} +22 \quad +22 \\ \hline \end{array}$$

$$\textcircled{39} = y$$

Alternate Interior

Angles are congruent.

Each angle is  
 $56^\circ$  or  $124^\circ$

$$\textcircled{3} \quad 3x = 2x+25$$

$$\begin{array}{r} -2x \quad -2x \\ \hline \end{array}$$

$$x = \textcircled{25}$$

corresponding angles  
are congruent.

Each angle is  $75^\circ$  or  $105^\circ$

$$\textcircled{4} \quad 3x-6 + 2x+26 = 180$$

$$5x+20 = 180$$

$$\begin{array}{r} -20 \quad -20 \\ \hline \end{array}$$

$$\frac{5x \neq 160}{5} \quad \frac{160}{5}$$

$$x = \textcircled{32}$$

same side Interior

Angles are Supplementary

Each angle is  $90^\circ$



$$\textcircled{5} \quad 5x + 7x - 20 = 180$$

$$12x - 20 = 180$$

$$\quad \quad \quad +20 \quad +20$$

$$\frac{12x}{12} = \frac{200}{12}$$

$$x = \textcircled{16.6667}$$

same side interior  
angles are supplementary

Each angle is  
 $83.333^\circ$  or  $96.6667^\circ$

$$\textcircled{6} \quad x + 5 = 9x - 16$$

$$-x \quad \quad \quad -x$$

$$5 = 8x - 16$$

$$\quad \quad \quad +16 \quad \quad \quad +16$$

$$\frac{21}{8} = \frac{8x}{8}$$

$$x = \textcircled{2.625}$$

Alternate Interior  
angles are congruent

Each angle is  
 $7.625^\circ$  or  $172.375^\circ$

$$\textcircled{7} \quad 3x + 9 = 7x - 30$$

$$-3x \quad \quad \quad -3x$$

$$9 = 4x - 30$$

$$\quad \quad \quad +30 \quad \quad \quad +30$$

$$\frac{39}{4} = \frac{4x}{4}$$

$$x = \textcircled{9.75}$$

Alternate Exterior  
Angles are congruent

Each angle is  
 $38.25^\circ$  or  $141.75^\circ$

$$\textcircled{8} \quad 2x + 4 = 3x - 10$$

$$-2x \quad \quad \quad -2x$$

$$4 = x - 10$$

$$\quad \quad \quad +10 \quad \quad \quad +10$$

$$\textcircled{14} = x$$

Alternate Interior  
Angles are congruent

Each angle is  
 $32^\circ$  or  $148^\circ$

$$\textcircled{9} \quad 5x - 10 = 3x + 50$$
$$\begin{array}{r} -3x \quad -3x \\ \hline 2x - 10 = 50 \\ +10 \quad +10 \\ \hline 2x = 60 \quad x = \textcircled{30} \end{array}$$

corresponding angles  
are congruent.

$$2x - 10 = 50$$
$$\begin{array}{r} +10 \quad +10 \\ \hline 2x = 60 \end{array}$$

Each angle is  
 $140^\circ$  or  $40^\circ$

$$\frac{2x}{2} = \frac{60}{2} \quad x = \textcircled{30}$$

$$\textcircled{10} \quad 2x + 5 + 3x = 180$$

supplementary  
Angles

$$5x + 5 = 180$$
$$\begin{array}{r} -5 \quad -5 \\ \hline 5x = 175 \end{array}$$

$$\frac{5x}{5} = \frac{175}{5} \quad x = \textcircled{35}$$

$$\textcircled{11} \quad 3x + x = 90$$

complementary  
angles

$$4x = 90$$
$$\frac{4x}{4} = \frac{90}{4}$$

$$x = \textcircled{22.5}$$

$$\textcircled{12} \quad 2x - 4 = x + 26$$

vertical angles  
are congruent.

$$\begin{array}{r} -x \quad -x \\ \hline x - 4 = 26 \\ +4 \quad +4 \\ \hline x = \textcircled{30} \end{array}$$

$$x - 4 = 26$$

$$\begin{array}{r} +4 \quad +4 \\ \hline x = 30 \end{array}$$

$$x = \textcircled{30}$$

$$\textcircled{13} \quad 3x - 20 + x + 40 = 180$$

$$4x + 20 = 180$$

$$\underline{-20 \quad -20}$$

$$\frac{4x = 160}{4 \quad 4}$$

$$x = \textcircled{40}$$

Linear Pairs

are Supplementary

$$\textcircled{14} \quad 7x - 12 = 2x + 3$$

$$\underline{-2x + 12 \quad -2x + 12}$$

$$\frac{5x = 15}{5 \quad 5}$$

$$x = \textcircled{3}$$

Alternate Interior

Angles are

congruent

$$\textcircled{15} \quad 5x - 20 = 4x + 7$$

$$\underline{-4x + 20 \quad -4x + 20}$$

$$x = \textcircled{27}$$

vertical angles

are congruent

$$\textcircled{16} \quad 3y + 6 + 4y + 6 = 180$$

$$7y + 12 = 180$$

$$\underline{-12 \quad -12}$$

$$\frac{7y = 168}{7 \quad 7}$$

$$y = \textcircled{24}$$

supplementary

angles

$$2x + 4 + 4y + 6 = 180$$

$$2x + 4 + 4(24) + 6 = 180$$

$$2x + 106 = 180$$

$$\underline{-106 \quad -106}$$

$$\frac{2x = 74}{2 \quad 2}$$

$$x = \textcircled{37}$$

$$\textcircled{17} \quad 3x + x - 10 = 180$$

$$4x = 190$$

$$\frac{4x = 190}{4 \quad 4}$$

$$x = \textcircled{47.5}$$

linear pairs are supplementary

# Review of Dilations

Name: \_\_\_\_\_

Period: \_\_\_\_\_ Date: \_\_\_\_\_

A **Dilation** is a transformation that produces an image that is the same shape as the original but different size.

- Dilations are similar to the original figure.
- Dilations are centered around the origin (0, 0), unless otherwise stated. (Point of Origin, "C")

Scale factor -- is  $\frac{\text{Dilated Image Length}}{\text{Original Image Length}}$ , which is a \_\_\_\_\_.

- If the scale factor is greater than 1, the figure becomes bigger. This is a Enlargement
- If the scale factor is between 0 and 1, the figure becomes smaller. This is a Reduction

**Example:** Would the following scale factors be an enlargement or a reduction?

1.  $\frac{5}{2}$  enlargement      2.  $\frac{1}{4}$  Reduction      3.  $\frac{2}{5}$  Reduction      4.  $\frac{2}{2}$  Neither      5.  $\frac{7}{3}$  Enlargement

**Rule:**  $(x, y) \rightarrow (kx, ky)$  where  $k$  represents scale factor. multiply the coordinates by the scale factor.

**Example 1:** Triangle  $ABC$  has vertices  $A(8, 1)$ ,  $B(2, 4)$ , and  $C(-2, 6)$ .  
What are the vertices of its dilated image with a scale factor of 2?

$A'$  (16, 2)       $B'$  (4, 8)       $C'$  (-4, 12)

**Example 2:** Triangle  $ABC$  has vertices  $A(0, 2)$ ,  $B(4, 4)$ , and  $C(-1, 4)$ .  
What are the vertices of its *image* with a scale factor of 4?

$A'$  (0, 8)       $B'$  (16, 16)       $C'$  (-4, 16)

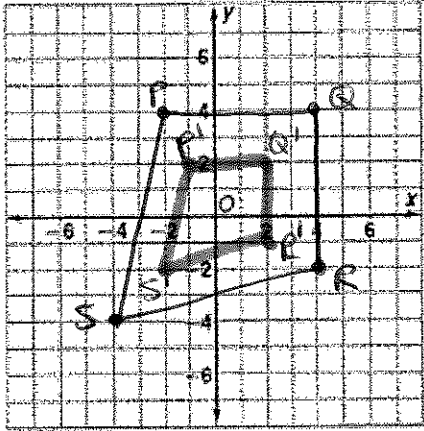
**Example 3:** Triangle  $ABC$  has vertices  $A(4, 12)$ ,  $B(-8, 4)$ , and  $C(-20, 0)$ .  
What are the vertices of its *image* with a scale factor of 1/4?

$A'$  (1, 3)       $B'$  (-2, 1)       $C'$  (-5, 0)

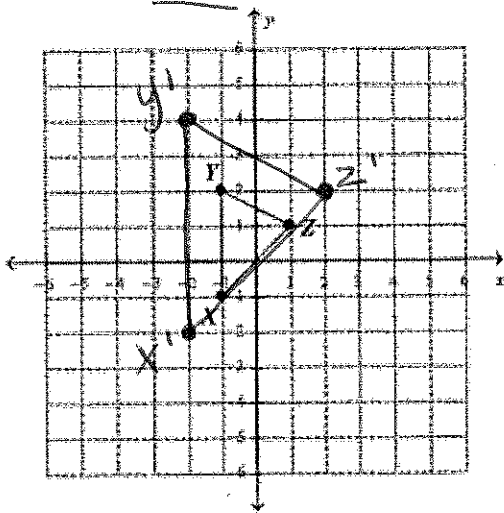
**Example 4:** Quadrilateral  $PQRS$  has vertices  $P(-2, 4)$ ,  $Q(4, 4)$ ,  $R(4, -2)$ , and  $S(-4, -4)$ . It is dilated by a scale factor of  $\frac{1}{2}$ .

$P'$   $(-1, 2)$      $Q'$   $(2, 2)$      $R'$   $(2, -1)$      $S'$   $(-2, -2)$

Graph the original image and the dilated image below.



**Example 5:** Triangle  $XYZ$  is graphed below. Draw and label Triangle  $X'Y'Z'$  after a dilation using a scale factor of two.



$X'$   $(-4, -4)$

$X'$   $(-2, -2)$

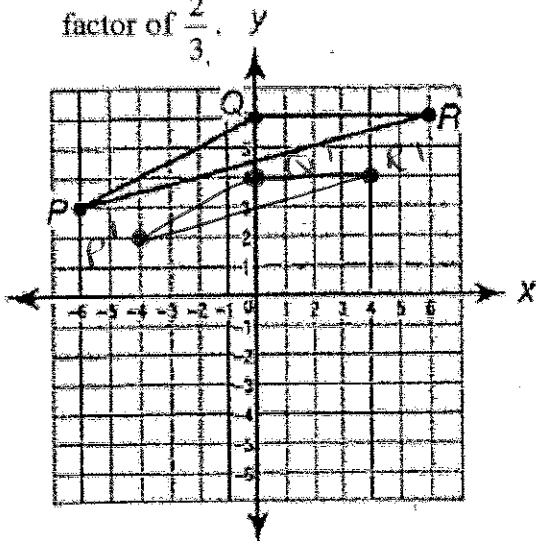
$Y'$   $(-4, 4)$

$Y'$   $(-2, 4)$

$Z'$   $(4, 4)$

$Z'$   $(2, 2)$

**Example 5:** Triangle  $PQR$  is graphed below. Draw and label Triangle  $P'Q'R'$  after a dilation using a scale factor of  $\frac{2}{3}$ .



$P'$   $(-4, 2)$

$P'$   $(-4, 2)$

$Q'$   $(0, 4)$

$Q'$   $(0, 4)$

$R'$   $(4, 4)$

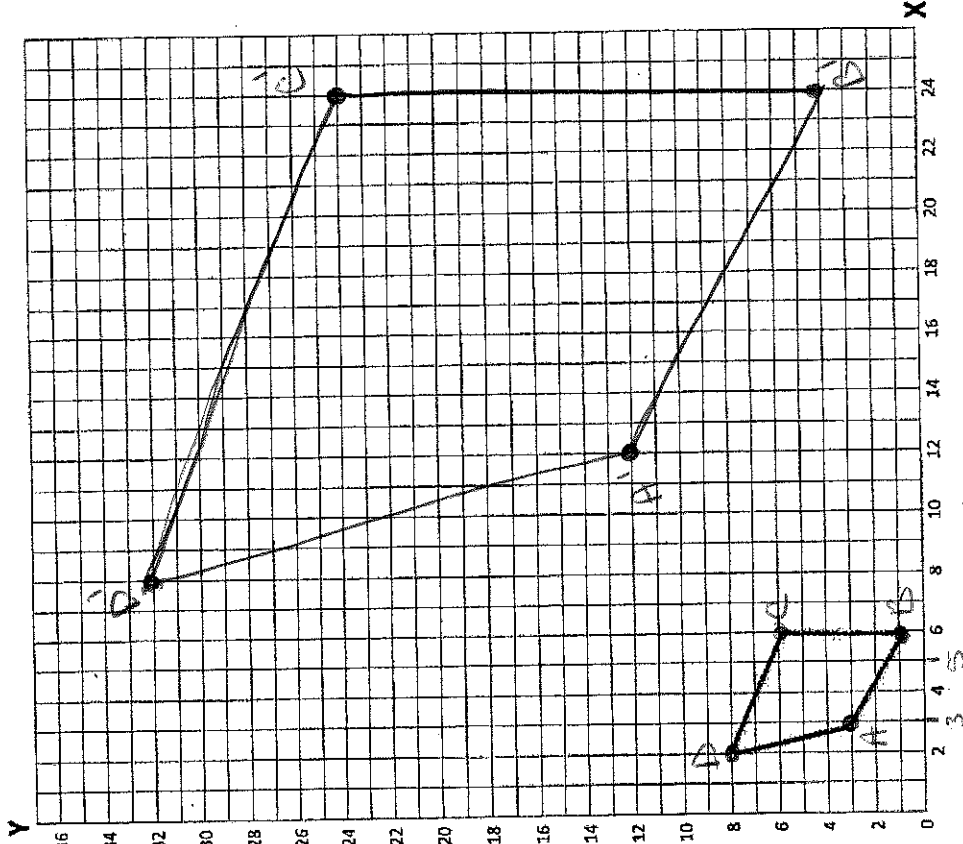
$R'$   $(4, 4)$

DILATIONS PRACTICE WORKSHEET

Name:

Date:

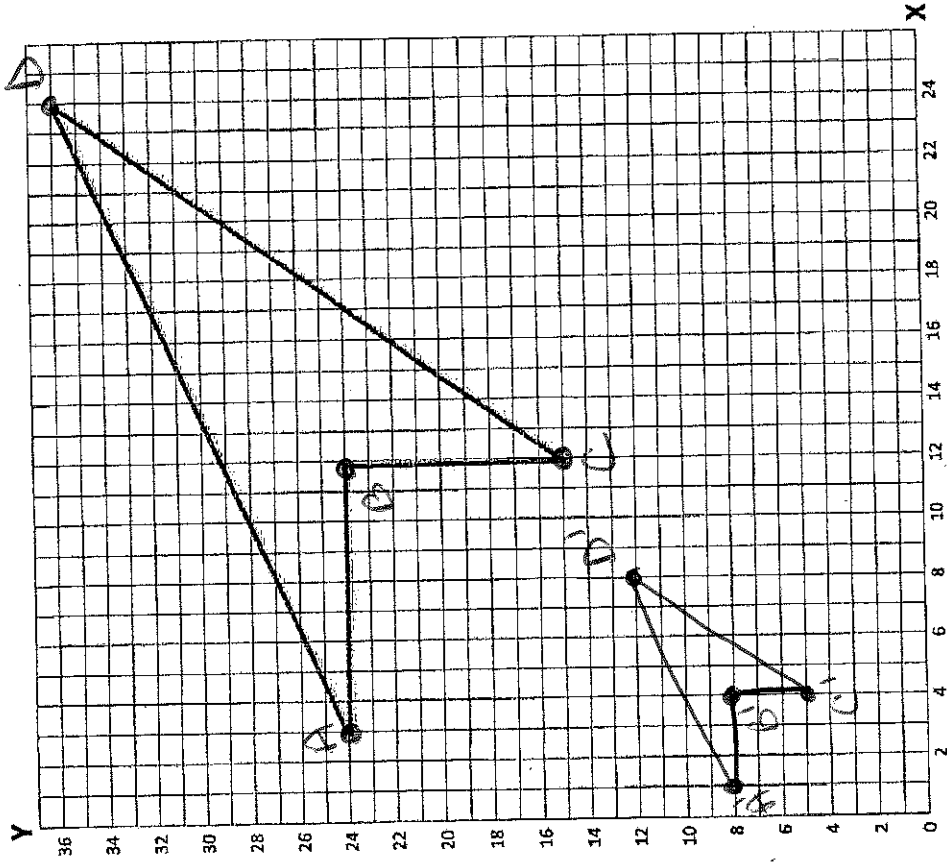
- Construct a dilation of the image with a scale factor of 4. Label the coordinates of the vertices.



- (10)
- A (3,3)
  - B (6,1)
  - C (6,6)
  - D (2,8)
  - A' (12,12)
  - B' (24,4)
  - C' (24,24)
  - D' (8,32)

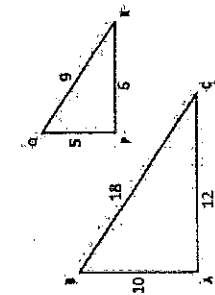
DILATIONS PRACTICE WORKSHEET (p. 2)

- Construct a dilation of the image with a scale factor of  $\frac{1}{3}$ . Label the coordinates of the vertices.



- (11)
- A (3,24)
  - B (12,24)
  - C (12,15)
  - D (8,12)
  - A' (1,8)
  - B' (4,8)
  - C' (4,5)
  - D' (8,12)

Similar Triangles



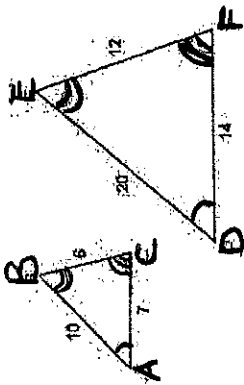
$$\frac{5}{10} = \frac{1}{2}$$

$$\frac{9}{18} = \frac{1}{2}$$

$$\frac{12}{24} = \frac{1}{2}$$

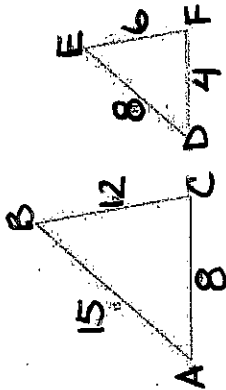
$\triangle ABC \sim \triangle PQR$   
by the  
SSS Similarity  
Theorem

10.



$\triangle ABC \sim \triangle DEF$   
by AA Similarity  
Postulate

11.



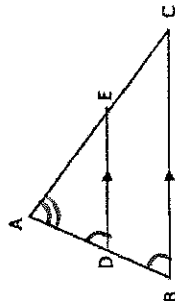
$$\frac{4}{8} = \frac{1}{2}$$

$$\frac{6}{12} = \frac{1}{2}$$

$$\frac{8}{15}$$

NOT  
similar  
because  
all 3 sides  
are not  
proportional

12.



$\triangle ADE \sim \triangle ABC$   
by AA Similarity postulate

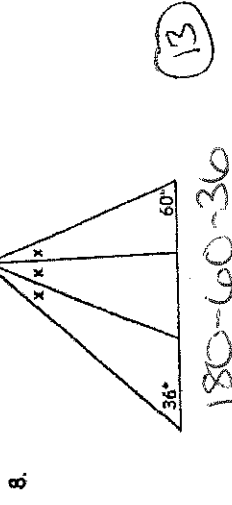
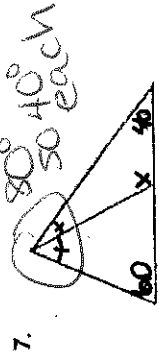
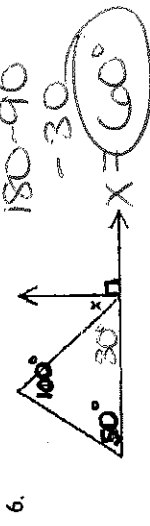
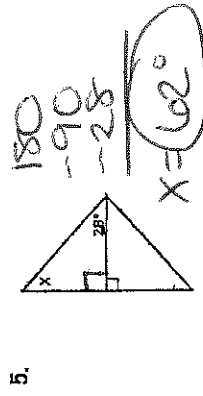
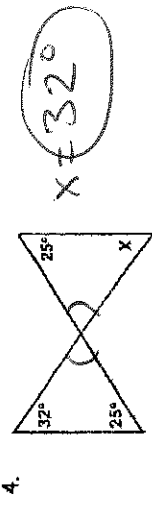
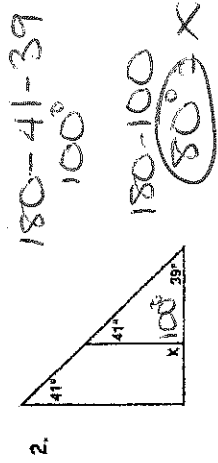
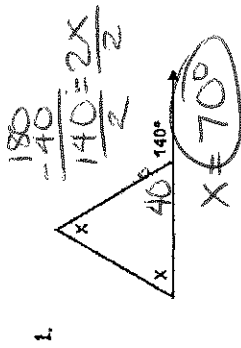
- \*  $\angle A$  is the same  $\angle$  in both triangles
- \*  $\angle D \cong \angle B$  because they are corresponding angles.

(12)

Geometry  
Worksheet

Name: \_\_\_\_\_  
Date: \_\_\_\_\_ Period: \_\_\_\_\_

Find x in each figure below. (\*\*Remember: The sum of three angles in any triangle is  $180^\circ$ \*\*)



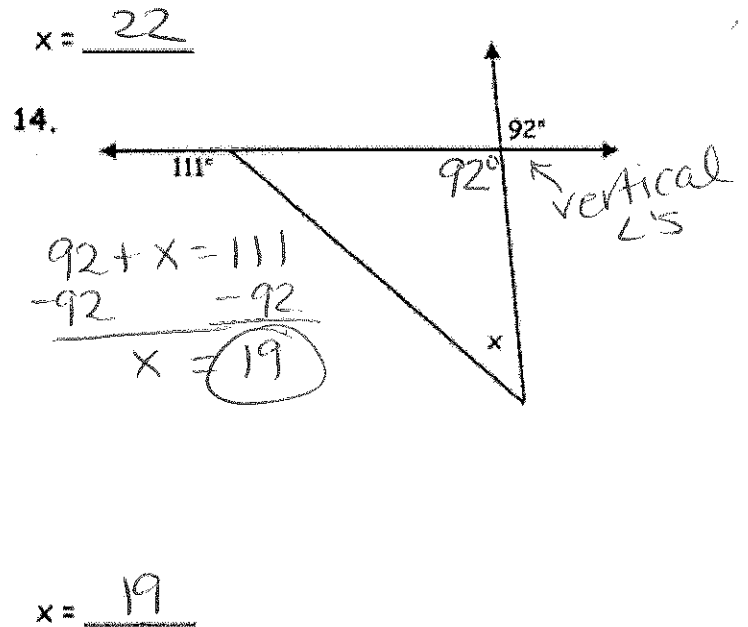
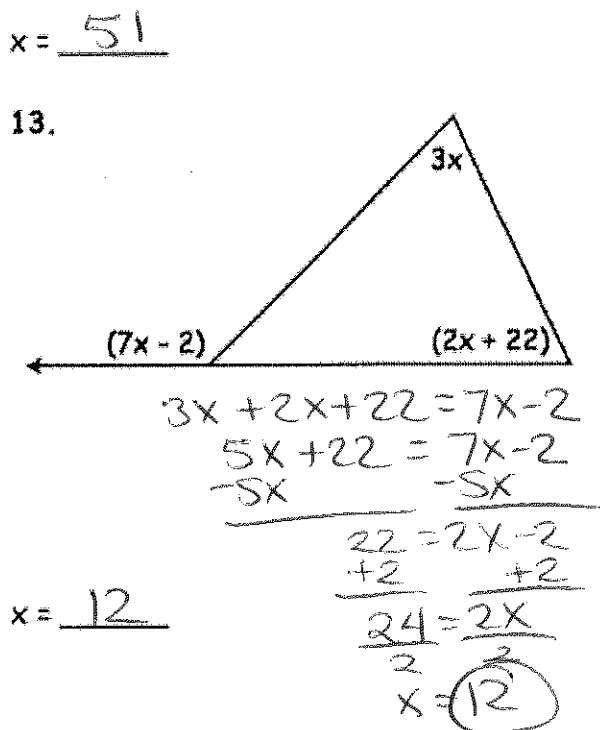
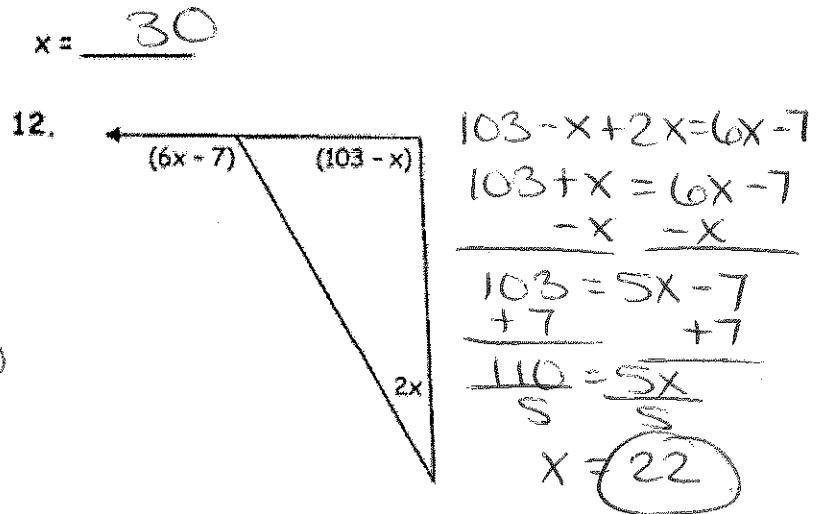
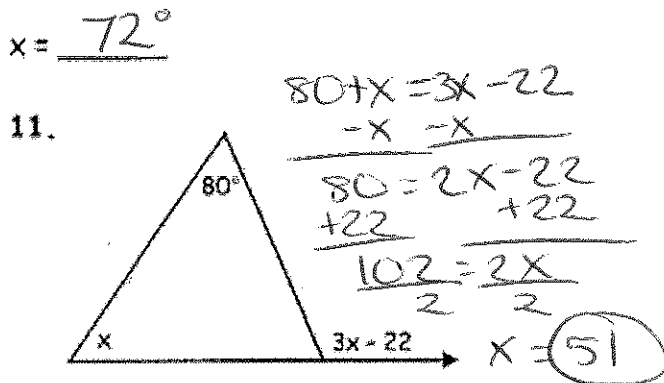
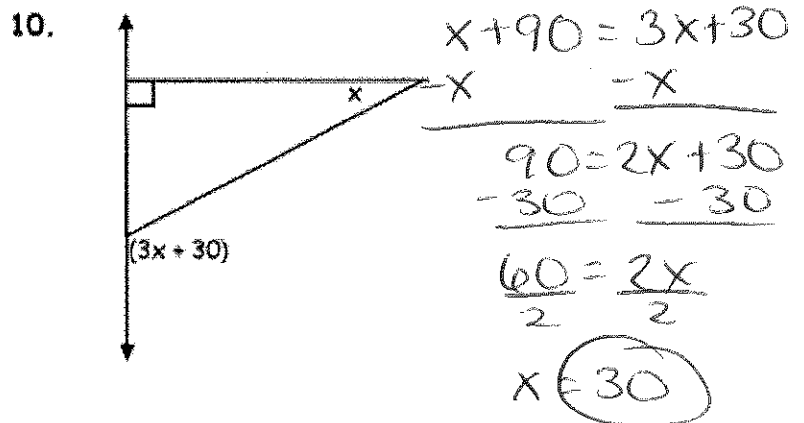
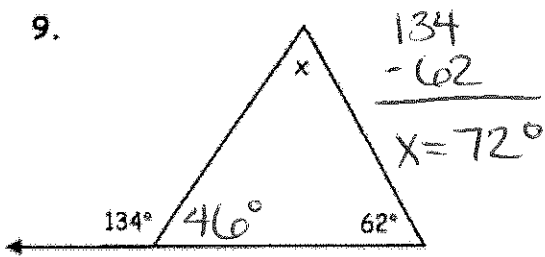
$$\frac{84}{3} = \frac{3x}{3}$$

$$x = 28$$

(13)

Rule:  $\text{Ext} + \text{L} = \text{Sum of 2 non-adj Interior L's}$

Find the value of  $x$  in each picture using the exterior angle theorem (in most cases).



$x = 19$

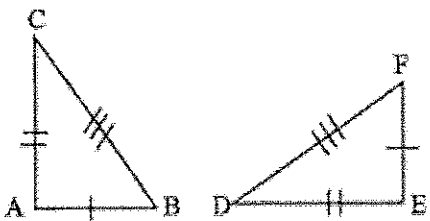


## Triangle Congruence Worksheet #1

For each pair of triangles, tell which postulates, if any, make the triangles congruent.

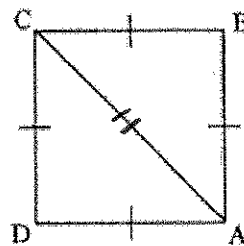
12.  $\triangle ABC \cong \triangle EFD$

SSS cong.



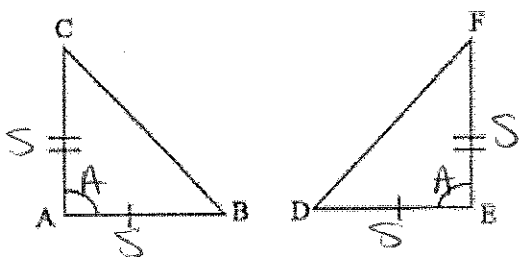
13.  $\triangle ABC \cong \triangle CDA$

SSS cong.



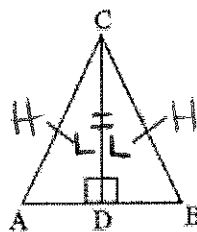
14.  $\triangle ABC \cong \triangle EFD$

SAS cong.



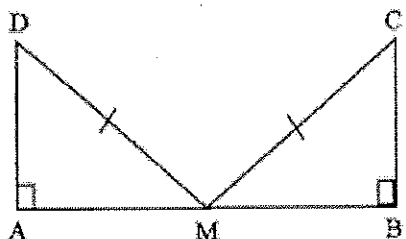
15.  $\triangle ADC \cong \triangle BDC$

HL cong.



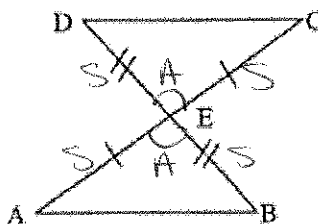
21.  $\triangle MAD \cong \triangle MBC$

\_\_\_\_\_



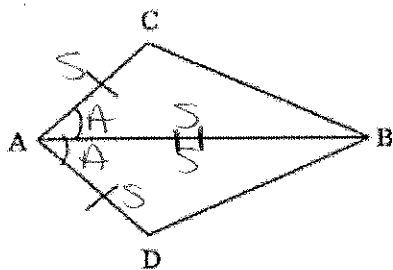
$\triangle ABE \cong \triangle CDE$

SAS cong.



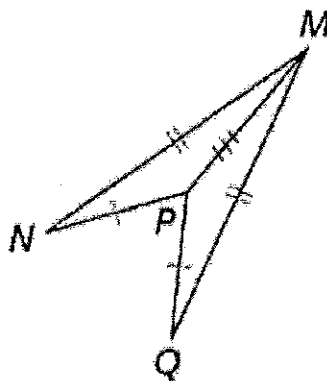
23.  $\triangle ACB \cong \triangle ADB$

SAS cong.



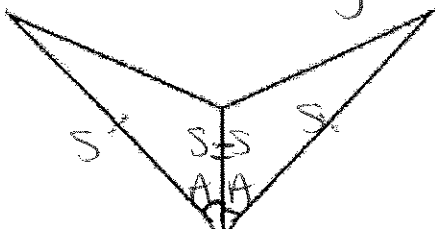
23.  $\triangle MNP \cong \triangle MQP$

SSS cong.



23.

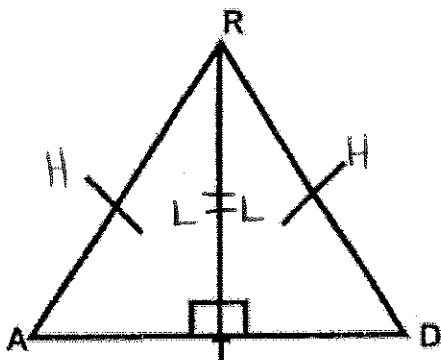
SAS cong.



## Right Triangle Congruence

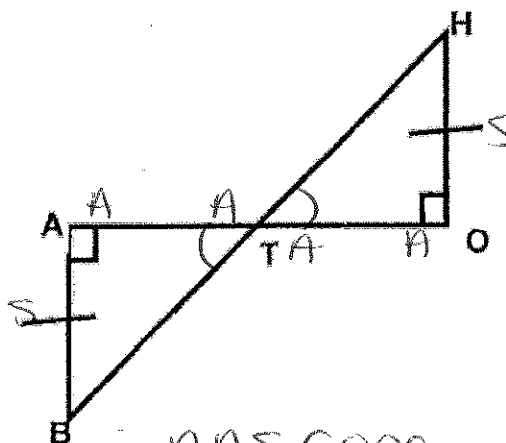
Is it possible to prove that the two triangles are congruent? If so, state the right triangle congruence theorem you would use to prove the two triangles are congruent and the congruence statement.

1.



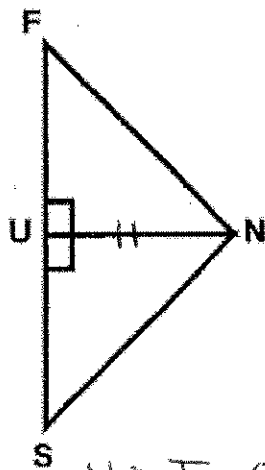
HL Cong.  
 $\triangle ATR \cong \triangle DTR$

2.



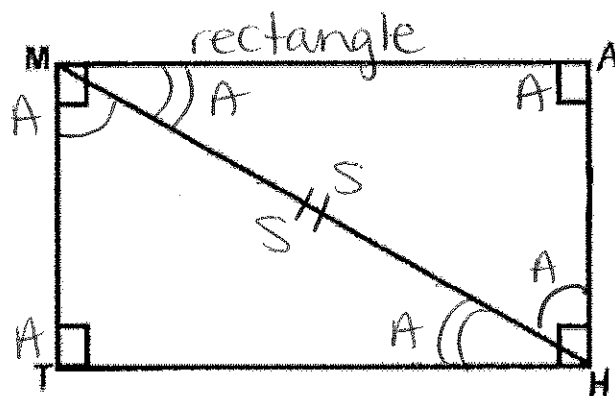
AAS Cong.  
 $\triangle BAT \cong \triangle HOT$

3.



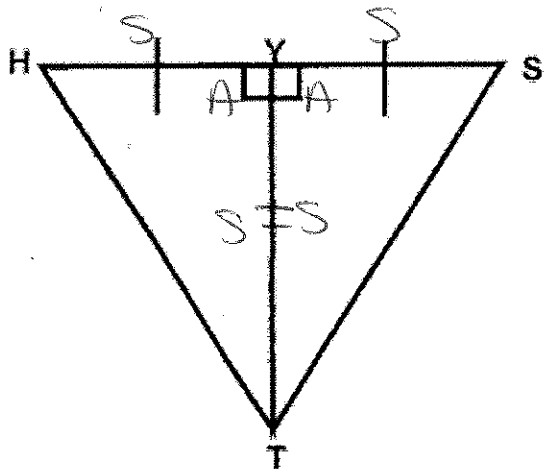
NOT congruent

4.



rectangle  
 AAS Cong or ASA Cong  
 $\triangle MTH \cong \triangle HAM$

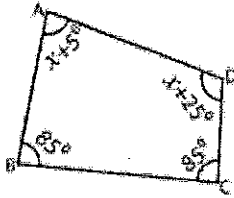
5.



SAS Cong.  
 $\triangle HyT \cong \triangle SyT$

**Angles in Quadrilateral**

Example:



Sum of the interior angles =  $360^\circ$

Sum of the interior angles =  $85^\circ + x + 25^\circ + x + 85^\circ + 85^\circ$

$360^\circ = 200^\circ + 2x$

$2x = 360^\circ - 200^\circ = 160^\circ$

$x = \frac{160^\circ}{2} = 80^\circ$

$\angle A = x + 5^\circ = 80^\circ + 5^\circ = 85^\circ$

$\angle D = x + 25^\circ = 80^\circ + 25^\circ = 105^\circ$

Find the missing angles in each quadrilateral.

1)  $2x + 140 = 360$   
 $\frac{-140}{2} \quad \frac{-140}{2}$   
 $2x = 220$   
 $x = 110$

$x = 110^\circ, \angle B = 110^\circ, \angle D = 115^\circ$

2)  $2x + 230 = 360$   
 $\frac{-230}{2} \quad \frac{-230}{2}$   
 $2x = 130$   
 $x = 65$

$x = 65, \angle R = 110^\circ, \angle S = 165^\circ$

3)  $2x + 200 = 360$   
 $\frac{-200}{2} \quad \frac{-200}{2}$   
 $2x = 160$   
 $x = 80$

$x = 80, \angle A = 105^\circ, \angle D = 75^\circ$

4)  $2x + 120 = 360$   
 $\frac{-120}{2} \quad \frac{-120}{2}$   
 $2x = 240$   
 $x = 120$

$x = 120, \angle I = 150^\circ, \angle J = 90^\circ$

5)  $2x + 230 = 360$   
 $\frac{-230}{2} \quad \frac{-230}{2}$   
 $2x = 130$   
 $x = 65$

$x = 65, \angle H = 65^\circ, \angle I = 70^\circ$

6)  $2x + 180 = 360$   
 $\frac{-180}{2} \quad \frac{-180}{2}$   
 $2x = 180$   
 $x = 90$

$x = 90, \angle W = 85^\circ, \angle Z = 80^\circ$

7)  $2x + 290 = 360$   
 $\frac{-290}{2} \quad \frac{-290}{2}$   
 $2x = 70$   
 $x = 35$

$x = 35, \angle Q = 72^\circ, \angle R = 75^\circ$

8)  $2x + 80 = 360$   
 $\frac{-80}{2} \quad \frac{-80}{2}$   
 $2x = 280$   
 $x = 140$

$x = 140, \angle P = 110^\circ, \angle S = 70^\circ$

9)  $3x + 210 = 360$   
 $\frac{-210}{3} \quad \frac{-210}{3}$   
 $3x = 150$   
 $x = 50$

$x = 50, \angle A = 60^\circ, \angle C = 130^\circ$

Name: \_\_\_\_\_

Date: \_\_\_\_\_

### The Properties of a Parallelogram

- Opposite sides are parallel.
- Opposite sides are congruent.
- Consecutive angles are supplementary.
- Opposite angles are congruent.
- Diagonals bisect each other.

The figure is a parallelogram. Find the value of  $x$ .



$$\begin{array}{r} 20 = 6x + 8 \\ -8 \quad -8 \\ \hline 12 = 6x \\ \div 6 \quad \div 6 \\ \hline 2 = x \end{array}$$

$x = 2$

The figure is a parallelogram. Find the value of  $x$ .



$$\begin{array}{r} 4x + 4 = 4x + 8 \\ -4x \quad -4x \\ \hline 4 = 8 \\ -4 \quad -4 \\ \hline 0 = 4 \end{array}$$

$x = 6$

The figure is a parallelogram. Find the value of  $x$ .



$$\begin{array}{r} 5x + 4 = 6x \\ -5x \quad -5x \\ \hline -4 = x \end{array}$$

$x = -12$

The figure is a parallelogram. Find the value of  $x$ .



$$\begin{array}{r} 9x + 96 = 180 \\ -96 \quad -96 \\ \hline 9x = 96 \\ \div 9 \quad \div 9 \\ \hline 10.66 = x \end{array}$$

$x = 84$

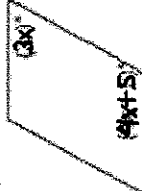
The figure is a parallelogram. Find the value of  $x$ .



$$\begin{array}{r} 2x - 1 = x + 4 \\ -2x \quad -2x \\ \hline -1 = x + 4 \\ -4 \quad -4 \\ \hline -5 = x \end{array}$$

$x = 5$

The figure is a parallelogram. Find the value of  $x$ .



$$\begin{array}{r} 3x + 4x + 5 = 180 \\ 7x + 5 = 180 \\ -5 \quad -5 \\ \hline 7x = 175 \\ \div 7 \quad \div 7 \\ \hline 25 = x \end{array}$$

$x = 25$

The figure is a parallelogram. Find the value of  $x$ .



$$\begin{array}{r} 9x - 31 = 4x - 1 \\ -4x \quad -4x \\ \hline 5x - 31 = -1 \\ +31 \quad +31 \\ \hline 5x = 30 \\ \div 5 \quad \div 5 \\ \hline 6 = x \end{array}$$

$x = 6$

### The Properties of a Rectangle

- Opposite sides are parallel.
- Opposite sides are congruent.
- Consecutive angles are supplementary.
- Opposite angles are congruent.
- All four angles are congruent (90°).
- Diagonals bisect each other.
- Diagonals are congruent.

8. A ABCD is a rectangle.  $AC = 33$ ,  $DB = 5x - 12$ . Find the value of  $x$ .



$$\begin{array}{r} 33 = 5x - 12 \\ +12 \quad +12 \\ \hline 45 = 5x \\ \div 5 \quad \div 5 \\ \hline 9 = x \end{array}$$

$x = 9$

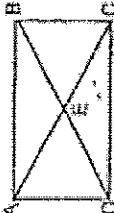
9. M MATH is a rectangle.  $m\angle H = (3x + 54)^\circ$ ,  $m\angle M = (3x + 54)^\circ$ . Find the value of  $x$ .



$$\begin{array}{r} 3x + 54 = 90 \\ -54 \quad -54 \\ \hline 3x = 36 \\ \div 3 \quad \div 3 \\ \hline 12 = x \end{array}$$

$x = 11.6667$

10. A ABCD is a rectangle.  $DE = 5x - 16$  &  $EC = 14 - 5x$ . Find the value of  $x$ .



$$\begin{array}{r} 5x - 16 = 14 - 5x \\ +5x \quad +5x \\ \hline 10x - 16 = 14 \\ +16 \quad +16 \\ \hline 10x = 30 \\ \div 10 \quad \div 10 \\ \hline 3 = x \end{array}$$

$x = 3$

11. The figure is a rectangle. Find the value of  $x$ .



$$\begin{array}{r} 2x - 9 = 5x + 12 \\ -2x \quad -2x \\ \hline -9 = 3x + 12 \\ -12 \quad -12 \\ \hline -21 = 3x \\ \div 3 \quad \div 3 \\ \hline -7 = x \end{array}$$

$x = -7$

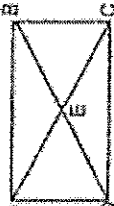
12. The figure is a rectangle. Find the value of  $x$ .



$$\begin{array}{r} 3x - 60 = 90 \\ +60 \quad +60 \\ \hline 3x = 150 \\ \div 3 \quad \div 3 \\ \hline 50 = x \end{array}$$

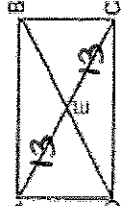
$x = 52$

13. A ABCD is a rectangle.  $DE = 28$ . Find the length of AC.



$$28(2) = 56$$

14. A MATH is a rectangle.  $AC = 26$  and  $EB = 2x - 5$ . Find the value of  $x$ .



$$\begin{array}{r} 2x - 5 = 13 \\ +5 \quad +5 \\ \hline 2x = 18 \\ \div 2 \quad \div 2 \\ \hline 9 = x \end{array}$$

$x = 9$