

UNIT 2

Trig Ratios:

$$\sin \theta = \frac{\text{opp}}{\text{Hyp}} \quad \cos \theta = \frac{\text{adj}}{\text{Hyp}} \quad \tan \theta = \frac{\text{opp}}{\text{adj}}$$

Finding missing sides:

- If x flies high... multiply
- If x is on the bottom... swap'm $\hat{=}$ divide

Finding missing angles:

- use inverse trig function

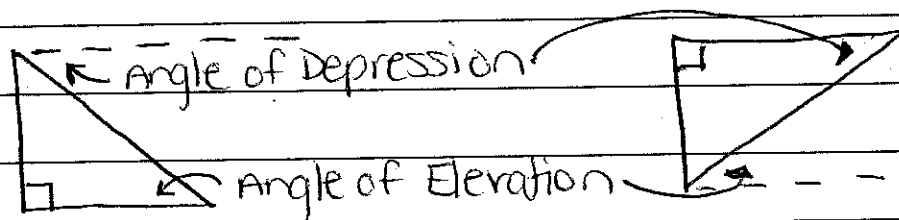
ex. [2nd] sin is $\sin^{-1} \left(\frac{\#}{\#} \right)$

Pythagorean Theorem $a^2 + b^2 = c^2$

- use to find 3rd side of a Δ

Other Properties:

- $\cos A = \sin B$
- $\cos A = \sin (90 - A)$
- $\sin A = \cos (90 - A)$

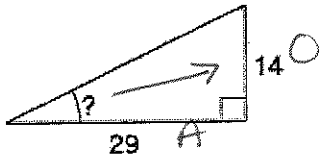


Angle of
Elevation &
Depression
have same
measures

TRIG BASICS

Find the missing side or angle:

1.



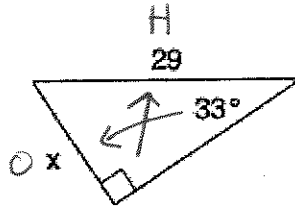
$$\tan \theta = \frac{O}{A}$$

$$\tan \theta = \frac{14}{29}$$

$$\tan^{-1} \left(\frac{14}{29} \right)$$

$$\theta = 25.769^\circ$$

2.



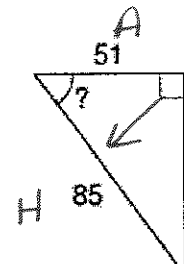
$$\sin 33 = \frac{O}{H}$$

$$\sin 33 = \frac{x}{29}$$

$$x = 29 \sin 33$$

$$x = 15.795$$

3.



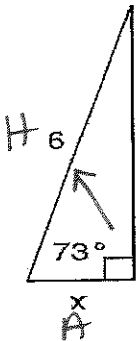
$$\cos \theta = \frac{A}{H}$$

$$\cos \theta = \frac{51}{85}$$

$$\cos^{-1} \left(\frac{51}{85} \right) =$$

$$\theta = 53.130^\circ$$

4.



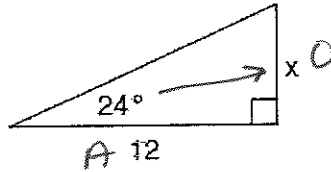
$$\cos 73 = \frac{A}{H}$$

$$\cos 73 = \frac{x}{6}$$

$$x = 6 \cos 73$$

$$x = 1.754$$

5.



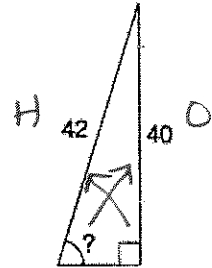
$$\tan 24 = \frac{O}{A}$$

$$\tan 24 = \frac{x}{12}$$

$$x = 12 \tan 24$$

$$x = 5.343$$

6.



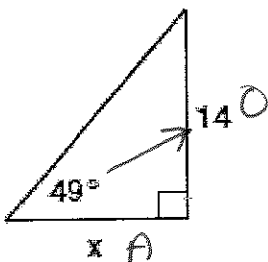
$$\sin \theta = \frac{O}{H}$$

$$\sin \theta = \frac{40}{42}$$

$$\sin^{-1} \left(\frac{40}{42} \right)$$

$$\theta = 72.247^\circ$$

7.



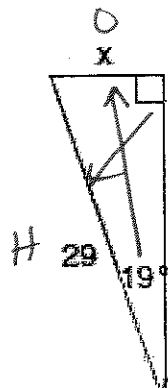
$$\tan 49 = \frac{O}{A}$$

$$\tan 49 = \frac{14}{x}$$

$$x = \frac{14}{\tan 49}$$

$$x = 12.170$$

8.



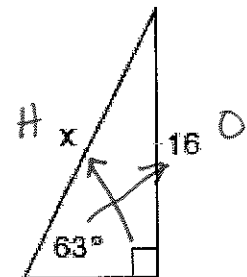
$$\sin 19 = \frac{O}{H}$$

$$\sin 19 = \frac{x}{29}$$

$$x = 29 \sin 19$$

$$x = 9.441$$

9.



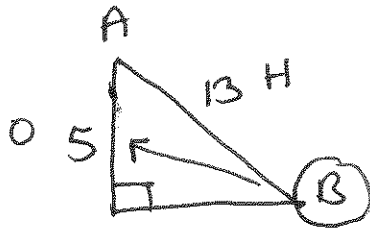
$$\sin 63 = \frac{16}{x}$$

$$x = \frac{16}{\sin 63}$$

$$x = 17.957$$

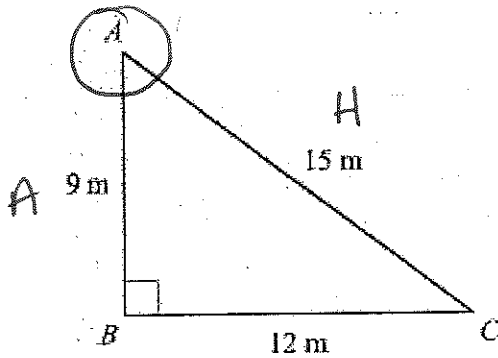
1. In right triangle ABC , angle A and angle B are complementary angles. The value of $\cos A$ is $\frac{5}{13}$. What is the value of $\sin B$?

- A. $\frac{5}{13}$
- B. $\frac{12}{13}$
- C. $\frac{13}{12}$
- D. $\frac{13}{5}$



$$\sin B = \frac{O}{H} = \frac{5}{13}$$

2. Triangle ABC is given below.



What is the value of $\cos A$? $\frac{A}{H}$

- A. $\frac{3}{5}$
- B. $\frac{3}{4}$
- C. $\frac{4}{5}$
- D. $\frac{5}{3}$

$$= \frac{9}{15} = \frac{3}{5}$$

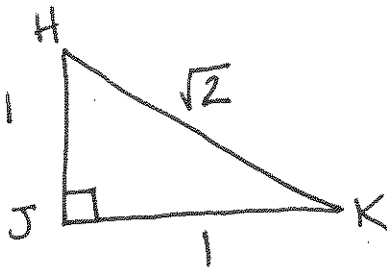
3. In right triangle HJK , $\angle J$ is a right angle and $\tan \angle H = 1$. Which statement about triangle HJK must be true?

~~A.~~ $\sin \angle H = \frac{1}{2} \frac{O}{H}$

~~B.~~ $\sin \angle H = 1 \frac{1}{\sqrt{2}}$

C. $\sin \angle H = \cos \angle H \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$

D. $\sin \angle H = \frac{1}{\cos \angle H}$



$$\tan H = \frac{O}{A} = 1$$

$$1^2 + 1^2 = C^2$$

$$2 = C^2$$

$$\sqrt{2} = C$$

4. A 12-foot ladder is leaning against a building at a 75° angle with the ground.

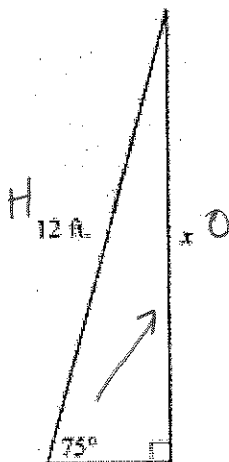
Which can be used to find how high the ladder reaches up the side of the building?

A. $\sin 75^\circ = \frac{12}{x}$

B. $\tan 75^\circ = \frac{12}{x}$

C. $\cos 75^\circ = \frac{x}{12}$

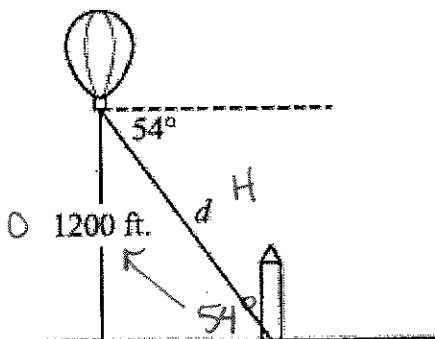
D. $\sin 75^\circ = \frac{x}{12}$



$$\sin 75 = \frac{0}{H}$$

$$\sin 75 = \frac{x}{12}$$

5. A hot air balloon is 1200 feet above the ground. The angle of depression from the basket of the hot-air balloon to the base of a monument is 54° .



Which equation can be used to find the distance, d , in feet, from the basket of the hot-air balloon to the base of the monument?

A. $\sin 54^\circ = \frac{d}{1200}$

$$\sin 54 = \frac{1200}{d}$$

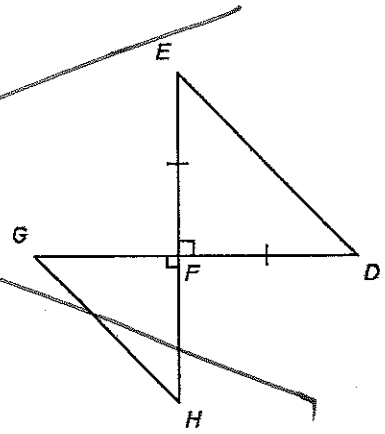
B. $\sin 54^\circ = \frac{1200}{d}$

C. $\cos 54^\circ = \frac{d}{1200}$

D. $\cos 54^\circ = \frac{1200}{d}$

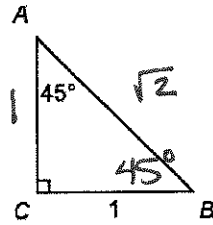
6. In the figure below, $\triangle DEF \sim \triangle GHF$. Which statements are true?

- A $\frac{FD}{EF} = \frac{FG}{HF}$ D $\frac{DE}{FD} = \sqrt{2}$
 B $\frac{HF}{FG} = 1$ E $\frac{DE}{EF} = \frac{GH}{HF}$
 C $\frac{FD}{FG} = 1$ F $\frac{FD}{DE} = \frac{GH}{FG}$



7. Use the figure shown to determine which of the statements below are true.

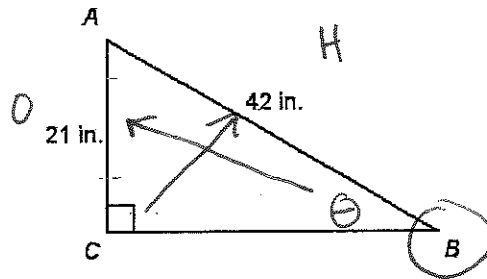
- A $\sin A = \cos B$ $\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$
 B $\sin A = \cos A$ $\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$
 C $\cos A = 1$ $\frac{1}{\sqrt{2}}$
 D $\sin B = \cos A$ $\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$
 E $\sin A = \frac{\sqrt{2}}{2} \cdot \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2}$



just like #3

8. A ramp that is being constructed must be 42 inches long and reach a ledge that is 21 inches tall. Which inverse trigonometric ratio could be used to find $m\angle B$?

- A $\sin^{-1}\left(\frac{21}{42}\right)$
 B $\sin^{-1}\left(\frac{42}{21}\right)$
 C $\cos^{-1}\left(\frac{21}{42}\right)$
 D $\sin^{-1}\left(\frac{21\sqrt{3}}{42}\right)$



$\sin \theta = \frac{21}{42}$
 $\sin^{-1}\left(\frac{21}{42}\right)$

Constructed Response:

9. Priya has planted a garden shaped like a right triangle. One leg of the triangle is 5 meters long, and the angle formed by it and the hypotenuse is 50° . If Priya wants to build a fence around her garden, how many meters of fence will she need? Round your answer to the nearest tenth.

$$\cos 50 = \frac{5}{x}$$

$$x = \frac{5}{\cos 50}$$

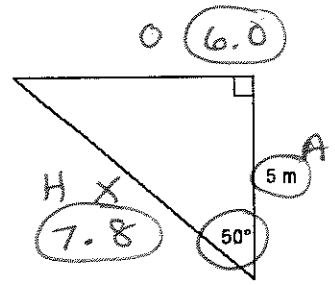
$$x = 7.8$$

$$\tan 50 = \frac{x}{5}$$

$$x = 5 \tan 50$$

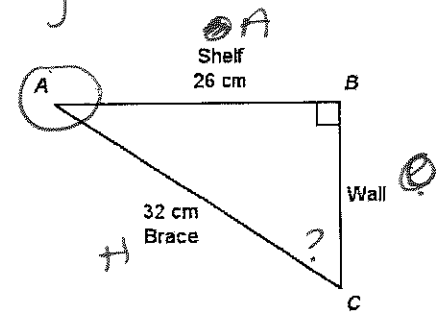
$$x = 6.0$$

$$\begin{array}{r} 6.0 \\ + 7.8 \\ + 5.0 \\ \hline 18.8 \text{ m} \end{array}$$



Priya will need 18.8m of fence around her garden.

10. A shelf extends perpendicularly 26 cm from a wall. You want to place a 32 cm brace under the shelf, as shown below.



- a. To the nearest tenth of a centimeter, how far below the shelf should the brace be attached to the wall? Show your work.

$$a^2 + b^2 = c^2$$

$$26^2 + b^2 = 32^2$$

$$676 + b^2 = 1024$$

$$\begin{array}{r} 676 + b^2 = 1024 \\ -676 \quad \quad -676 \\ \hline b^2 = 348 \end{array}$$

$$\begin{array}{l} \rightarrow b = \sqrt{348} \\ = 18.7 \text{ cm} \end{array}$$

The brace should be attached to the wall 18.7 cm below the shelf.

- b. To the nearest degree, what angle does the brace make with the wall? Show your work.

$$\sin C = \frac{26}{32}$$

$$C = \sin^{-1}\left(\frac{26}{32}\right)$$

$$C = 54^\circ$$

The brace makes a 54° angle with the wall.

- c. To the nearest degree, what angle does the brace make with the shelf? Show your work.

$$\cos A = \frac{26}{32}$$

$$A = \cos^{-1}\left(\frac{26}{32}\right)$$

$$A = 36^\circ$$

The brace makes a 36° angle with the shelf.