

## UNIT 7

Probability:  $P = \frac{\text{ASK}}{\text{Total}}$

Symbols: U = OR (add)  
n = And (multiply)

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

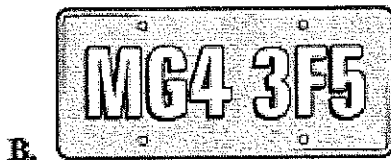
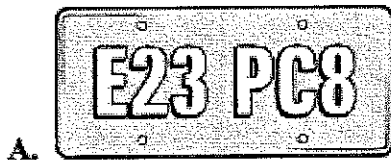
$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

\* subtract out duplicates

$$P(A|B) = \frac{P(A \text{ and } B)}{P(B)}$$

1. In a particular state, the first character on a license plate is always a letter. The last character is always a digit from 0 to 9.

If  $V$  represents the set of all license plates beginning with a vowel, and  $O$  represents the set of all license plates that end with an odd number, which license plate belongs to the set  $V \cap O$ ?



2. Which of the following events are independent given  $P(A)$ ,  $P(B)$ , and  $P(A \text{ and } B)$ ?

- ~~X~~ A.  $P(A) = 0.25$ ;  $P(B) = 0.25$ ;  $P(A \text{ and } B) = 0.5$      $0.25(0.25) = 0.0625$   
~~X~~ B.  $P(A) = 0.08$ ;  $P(B) = 0.4$ ;  $P(A \text{ and } B) = 0.12$      $0.08(0.4) = 0.032$   
~~X~~ C.  $P(A) = 0.16$ ;  $P(B) = 0.24$ ;  $P(A \text{ and } B) = 0.32$      $0.16(0.24) = 0.0384$   
 D.  $P(A) = 0.3$ ;  $P(B) = 0.15$ ;  $P(A \text{ and } B) = 0.045$      $0.3(0.15) = 0.045$  ✓

3. Assume that the following events are independent:

- The probability that a high school senior will go to college is 0.72.
- The probability that a high school senior will go to college and live on campus is 0.46.

What is the probability that a high school senior will live on campus, given that the person will go to college?

- A. 0.26  
 B. 0.33  
 C. 0.57  
 D. 0.64

college = .72  
 college / live on campus = .46  
 $P(\text{live on campus out of all college})$   
 $\frac{.46}{.72} = 0.638$

4. A random survey was conducted about gender and hair color. This table records the data.

Hair Color

	Brown	Blonde	Red
Male	548	876	82
Female	612	716	66

only use males

What is the probability that a randomly selected person has blonde hair, given that the person selected is male?

- A. 0.51  
 B. 0.55  
 C. 0.58  
 D. 0.63

$$\frac{\text{blond}}{\text{males}} = \frac{876}{1506} = 0.58$$

5. Mrs. Klein surveyed 240 men and 285 women about their vehicles. Of those surveyed, 155 men and 70 women said they own a red vehicle. If a person is chosen at random from those surveyed, what is the probability of choosing a woman or a person that does NOT own a red vehicle?

- A.  $\frac{14}{57}$   
 B.  $\frac{71}{105}$   
 C.  $\frac{74}{105}$   
 D.  $\frac{88}{105}$

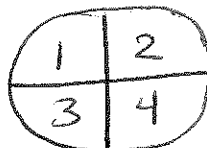
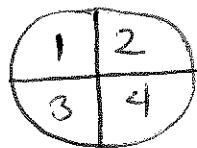
men = 240 } women = 285 } 525 Total  
 155 have a red car } 70 have a red car } 225 total with a red car

women } don't have red car } women without red car

$$\frac{285}{525} + \frac{300}{525} - \frac{215}{525} = \frac{74}{105}$$

6. Bianca spins two spinners that have four equal sections numbered 1 through 4. If she spins a 4 on at least one spin, what is the probability that the sum of her two spins is an odd number?

- A.  $\frac{1}{4}$   
 B.  $\frac{7}{16}$   
 C.  $\frac{4}{7}$   
 D.  $\frac{11}{16}$



- 11 21 31 41  
 12 22 32 42  
 13 23 33 43  
 14 24 34 44

prob given  $\frac{\text{ask}}{\text{total}}$

$$\frac{4}{7}$$

7. Each letter of the alphabet is written on a card using a red ink pen and placed in a container. Each letter of the alphabet is also written on a card using a black ink pen and placed in the same container. A single card is drawn at random from the container. What is the probability that the card has a letter written in black ink, the letter A, or the letter Z?

A.  $\frac{1}{2}$

**B.  $\frac{7}{13}$**

C.  $\frac{15}{26}$

D.  $\frac{8}{13}$

$$= \frac{26}{52} + \frac{1}{52} + \frac{1}{52}$$

$$= \frac{28}{52} = \frac{7}{13}$$

remember the back A and Z were counted already so only count the reds.

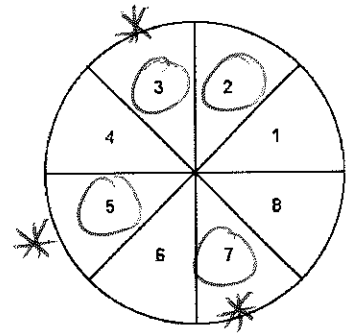
8. You spin a spinner with 8 equally likely landing spaces numbered 1 to 8. Event A is landing on a prime number. Event B is landing on an odd number. What is the intersection of A and B?

**A.  $\emptyset$**

C. {1, 2, 3, 5, 7}

**B. {3, 5, 7}**

D. {1, 2, 3, 4, 5, 6, 7, 8}



9. For two independent events A and B,  $P(A) = 0.5$  and  $P(B) = 0.4$ . What is  $P(A \text{ and } B)$ ?

**A. 0.1**

C. 0.8

**B. 0.2**

D. 0.9

$$= 0.5(0.4) = 0.20$$

10. In a bag of 20 candies, 12 are red and 15 have peanuts in them. If the events of picking a red candy and picking a candy with peanuts are independent, how many of the red candies have peanuts?

**A. 3**

**C. 9**

B. 6

D. 12

$$\frac{12}{20} \cdot \frac{15}{20} = \frac{9}{20}$$

11. Suppose events A and B are independent,  $P(A) = 0.75$ , and  $P(B) = 0.5$ . What is  $P(A | B)$ , the probability of A given B?

**A. 0.25**

**C. 0.5**

B. 0.375

**D. 0.75**

$$\frac{0.75(0.5)}{0.5} = 0.75$$

12. Darren randomly chooses a card from a standard deck of 52 playing cards. What is the probability that Darren chooses a club or a queen?

**A.  $\frac{4}{52}$**

B.  $\frac{13}{52}$

**C.  $\frac{16}{52}$**

D.  $\frac{17}{52}$

$$\frac{13}{52} + \frac{4}{52} - \frac{1}{52} = \frac{16}{52}$$

use formula on formula sheet

## CONSTRUCTED RESPONSE

1. A fair number cube is rolled two times. Are the events that the first roll is an even number and the second roll is a 6 independent? Justify your answer.

yes... the first roll does not influence the second roll.

2. 16 cards numbered 1 through 16 are placed face down and Stephanie chooses one at random. What is the probability that the number on Stephanie's card is less than 5 or greater than 10? Show your work.

$$\frac{4}{16} + \frac{6}{16} = \frac{10}{16} = \frac{5}{8} = 0.625$$

3. Two-way frequency tables summarize data in two categories. These tables can be used to show if the two events are independent and to approximate conditional probabilities.

A random survey was taken to gather information about grade level and car ownership status of students at a school. This table shows the results of the survey.

	Owens a Car	Does Not Own a Car	Total
Junior	6	10	16
Senior	12	8	20
Total	18	18	36

Estimate the probability that a randomly selected student will be a junior, given that the student owns a car.

$$\frac{6 \text{ junior}}{18 \text{ own car}} = \frac{1}{3} \text{ or } .33$$

